

# 光の特性

## シンクロトロン放射とその特性

自然科学研究機構分子科学研究所  
総合研究大学院大学物理科学研究科

加藤政博

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- What is Synchrotron Light Source?
- Characteristics of Synchrotron Radiation
- Advanced Technologies
  - Towards High Brightness
  - Towards Coherence

# Contents

- *What is Synchrotron Light Source?*
- Characteristics of Synchrotron Radiation
- Advanced Technologies
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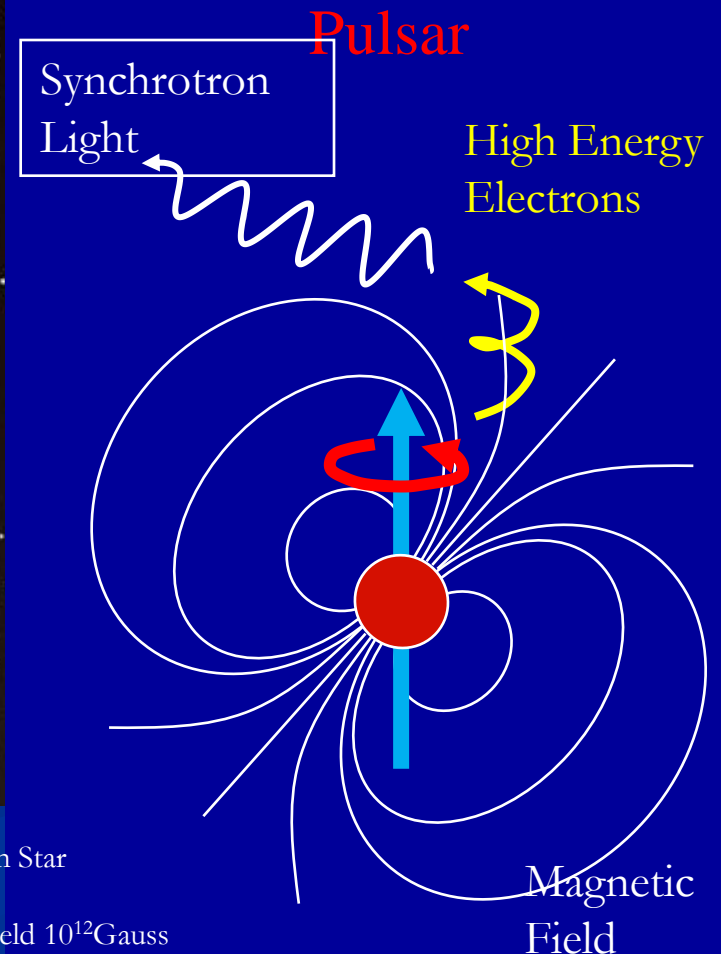
# Synchrotron Light Source in the Sky

Crab Nebula; A Super-nova Remnant  
The super-nova explosion was observed in AD1054.



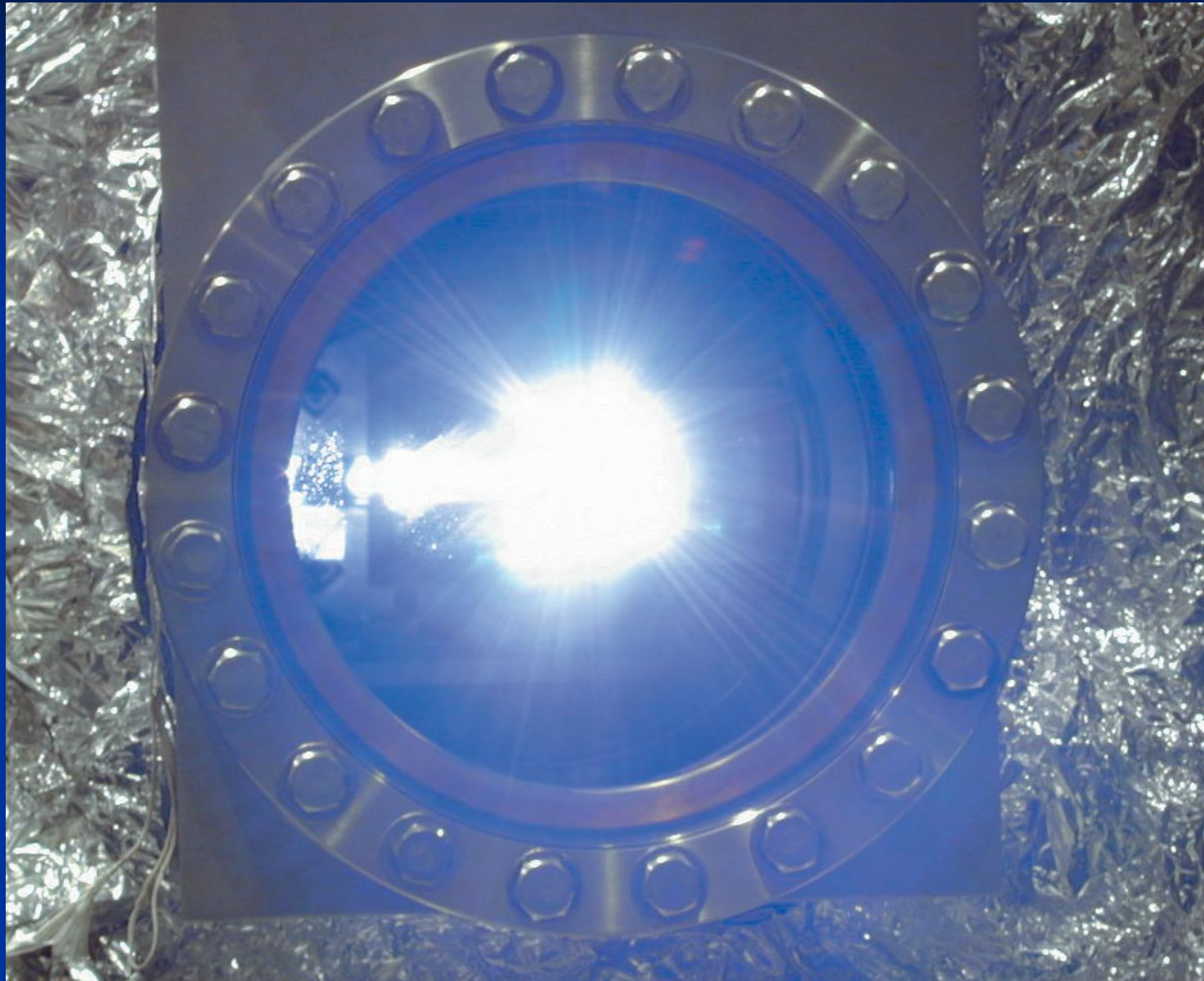
<http://www.nasa.gov/multimedia/imagegallery/>

What is Pulsar?  
Magnetized Neutron Star  
Diameter 10 km  
Surface Magnetic Field  $10^{12}$  Gauss  
Rotating Period 33 msec

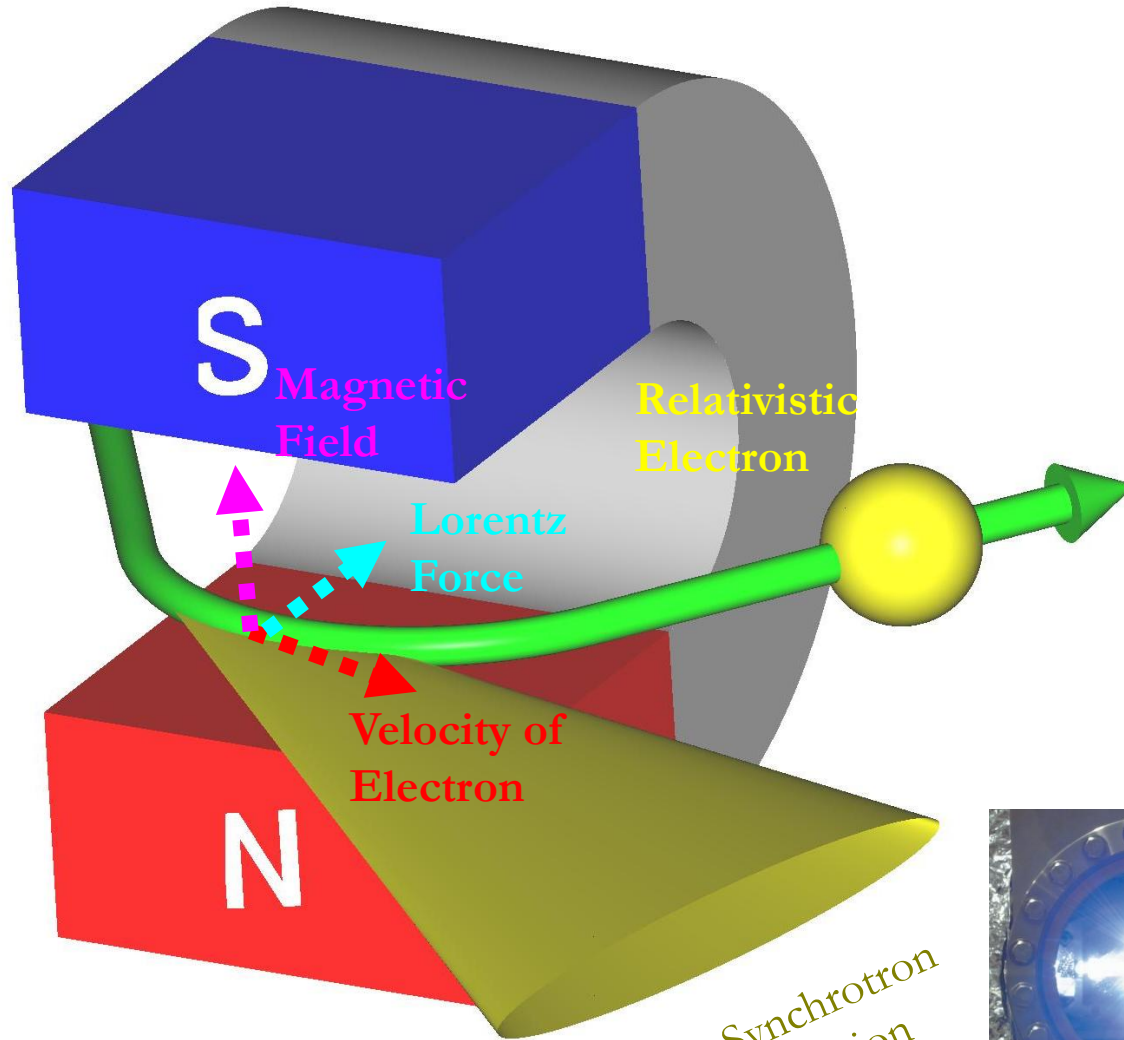




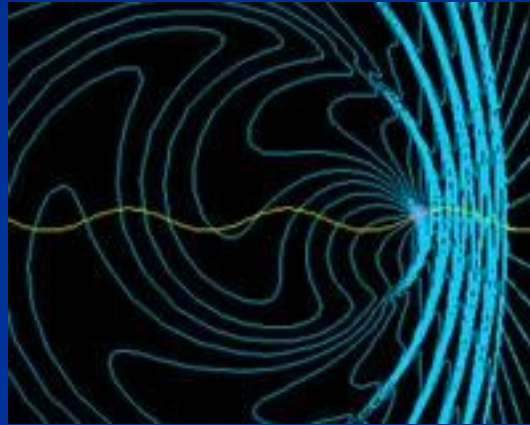
# Synchrotron Light Source on the Earth



# Synchrotron Radiation



# Radiation Simulator



<http://www-xfel.spring8.or.jp/dlmonitor.html>

# What are needed to produce synchrotron light?

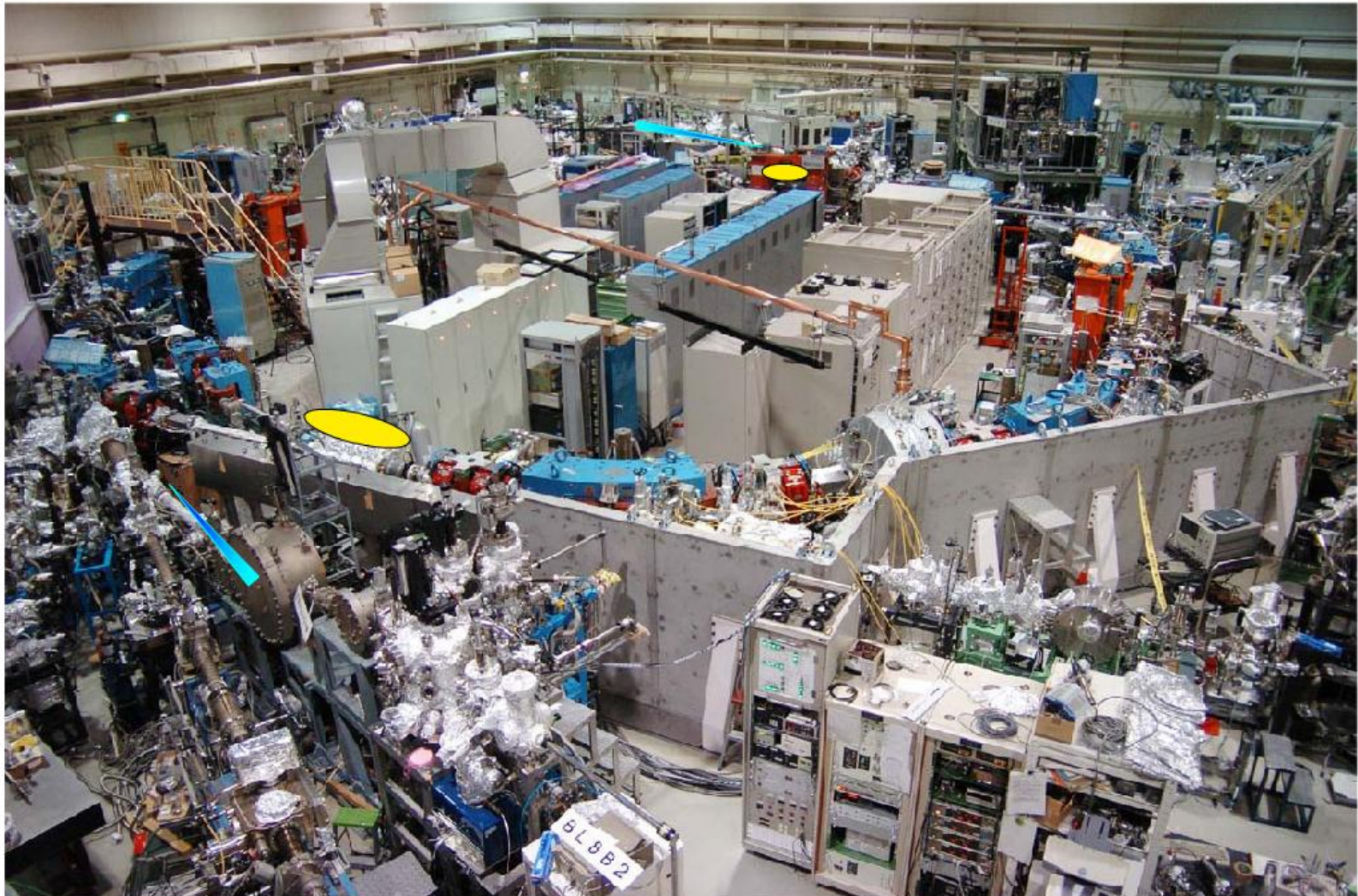
- High Energy Electrons
  - $\sim 0.5$  to  $\sim 10$  GeV
- Strong Magnetic Field
  - $\sim 1$  to  $\sim 10$  Tesla ( $= 10^4 \sim 10^5$  Gauss)
- Ultra-high Vacuum
  - $10^{-7} \sim 10^{-8}$  Pa



# UVSOR-II

Institute for Molecular Science, Okazaki, Japan

Circumference 53m, Electron Energy 750MeV



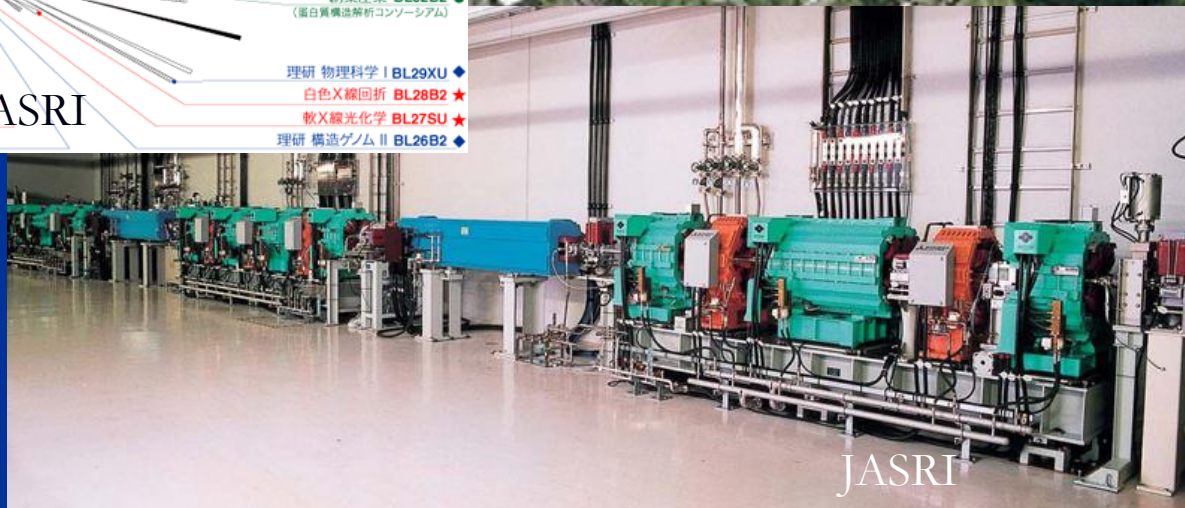
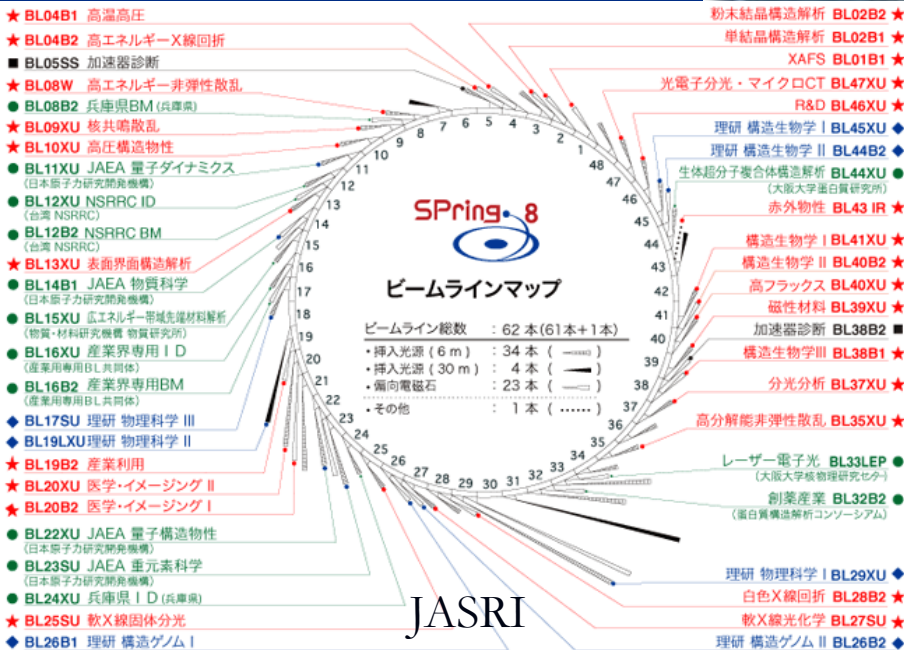


# SPring-8 (Nishi-Harima, Japan)

<http://www.spring8.or.jp>

Circumference; 1436 m

Electron Energy; 8 GeV



JASRI

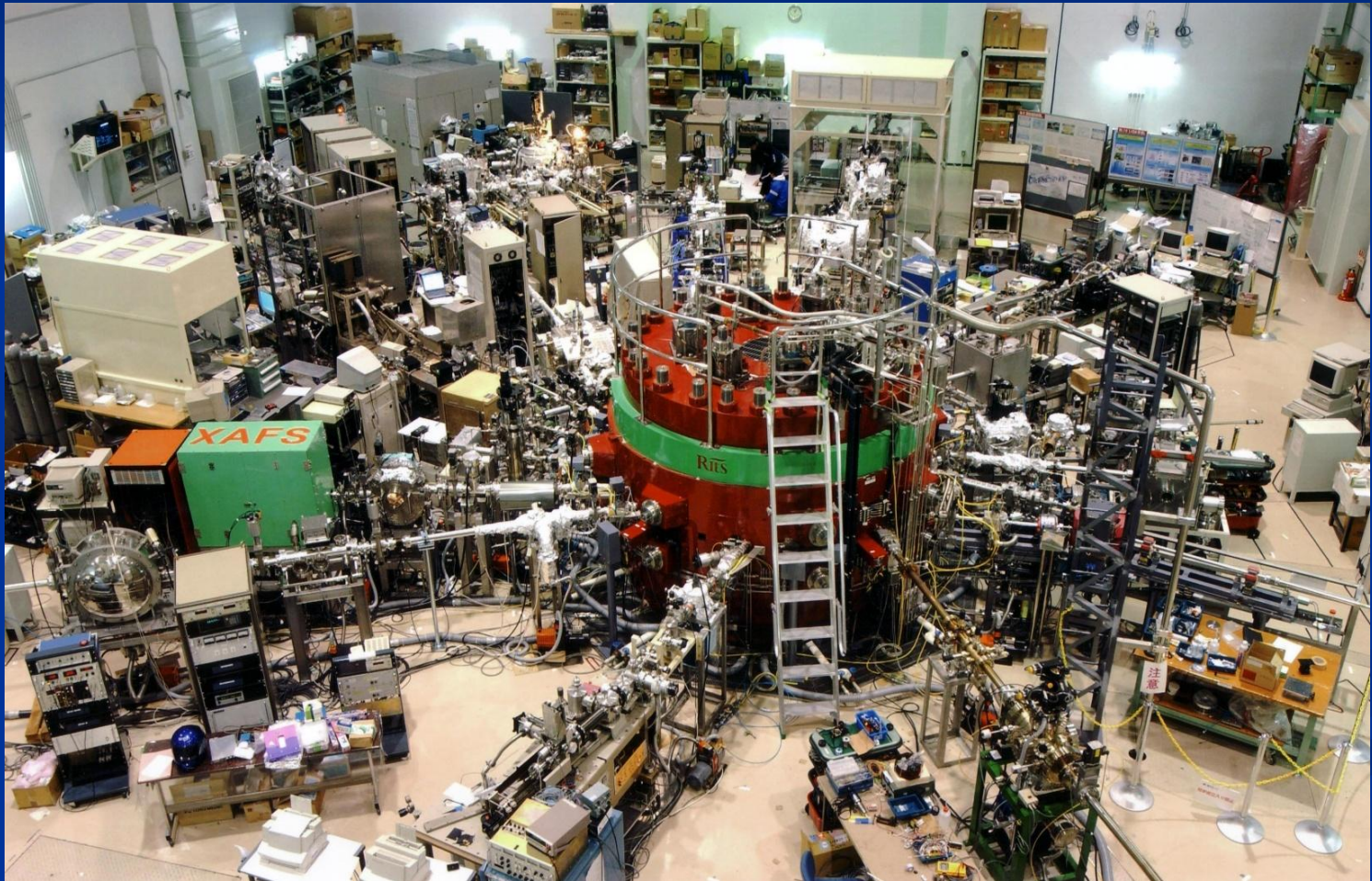
JASRI



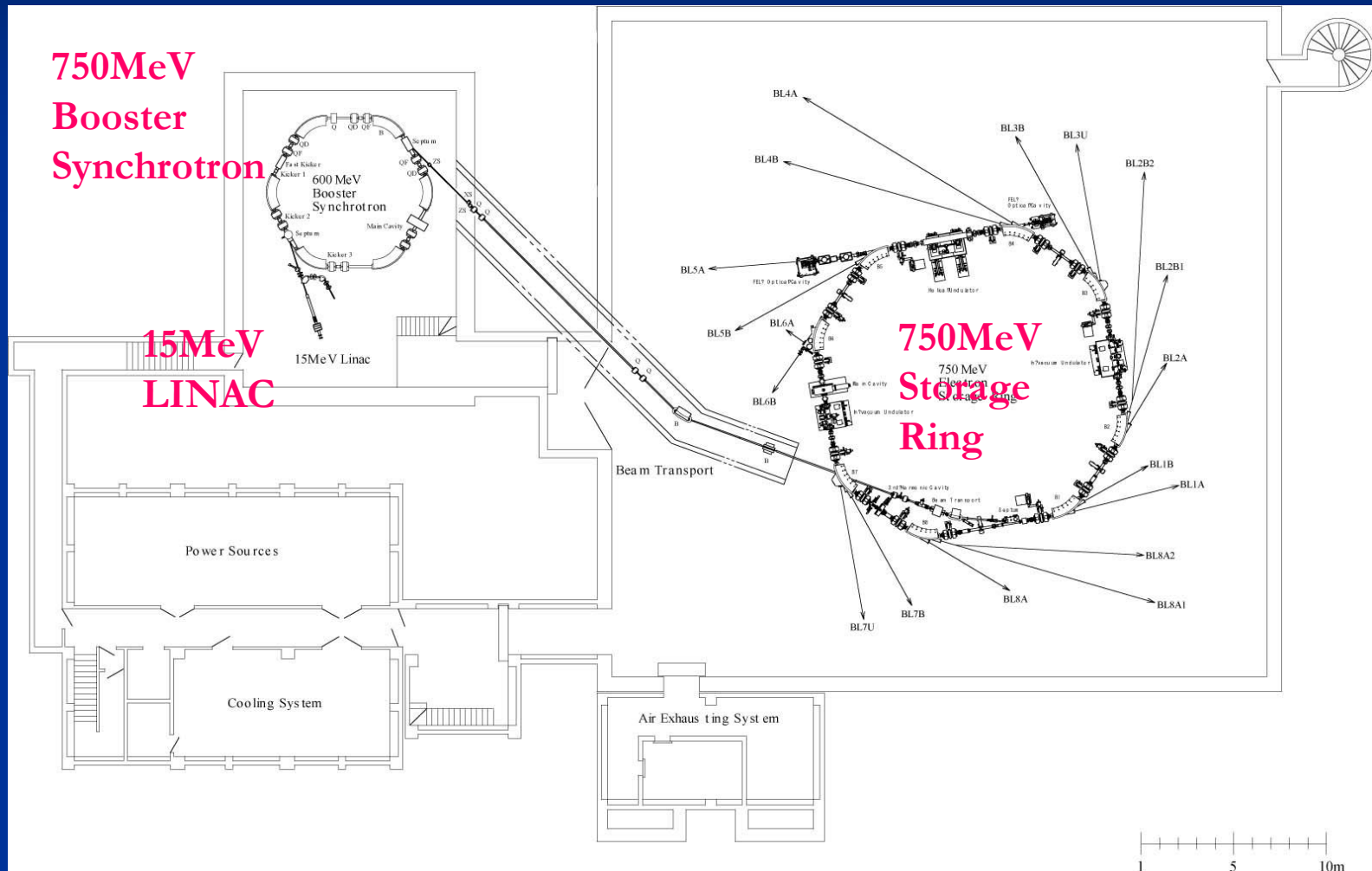
# AURORA (Ritsumeikan Univ.)

<http://www.ritsumei.ac.jp/acd/re/src/index.htm>

Circumference; 3 m, Electron Energy; 575 MeV



# Layout of Synchrotron Light Source UVSOR-II at Institute for Molecular Science

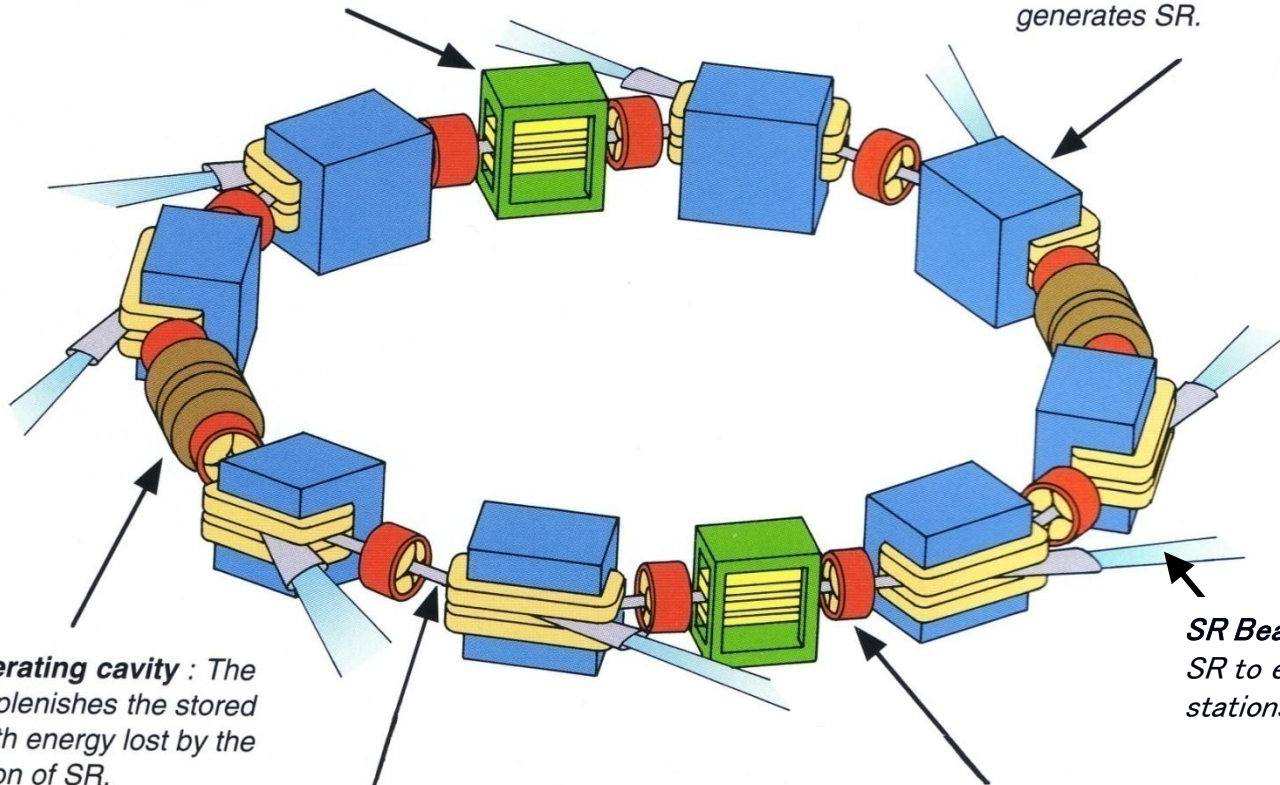




# Configuration of Electron Storage Ring

**ID** : The insertion device generates various characteristic types of SR.

**BM** : The bending magnet bends the beam and generates SR.



**rf accelerating cavity** : The cavity replenishes the stored beam with energy lost by the generation of SR.

**SR Beam Line** : guiding SR to experimental stations

**Vacuum Duct** : The pressure in the duct is kept below  $10^{-10}$  Torr in order to reduce beam decay caused by collisions with residual gas.

**QM** : The quadrupole magnet works as a lens to focus the beam.

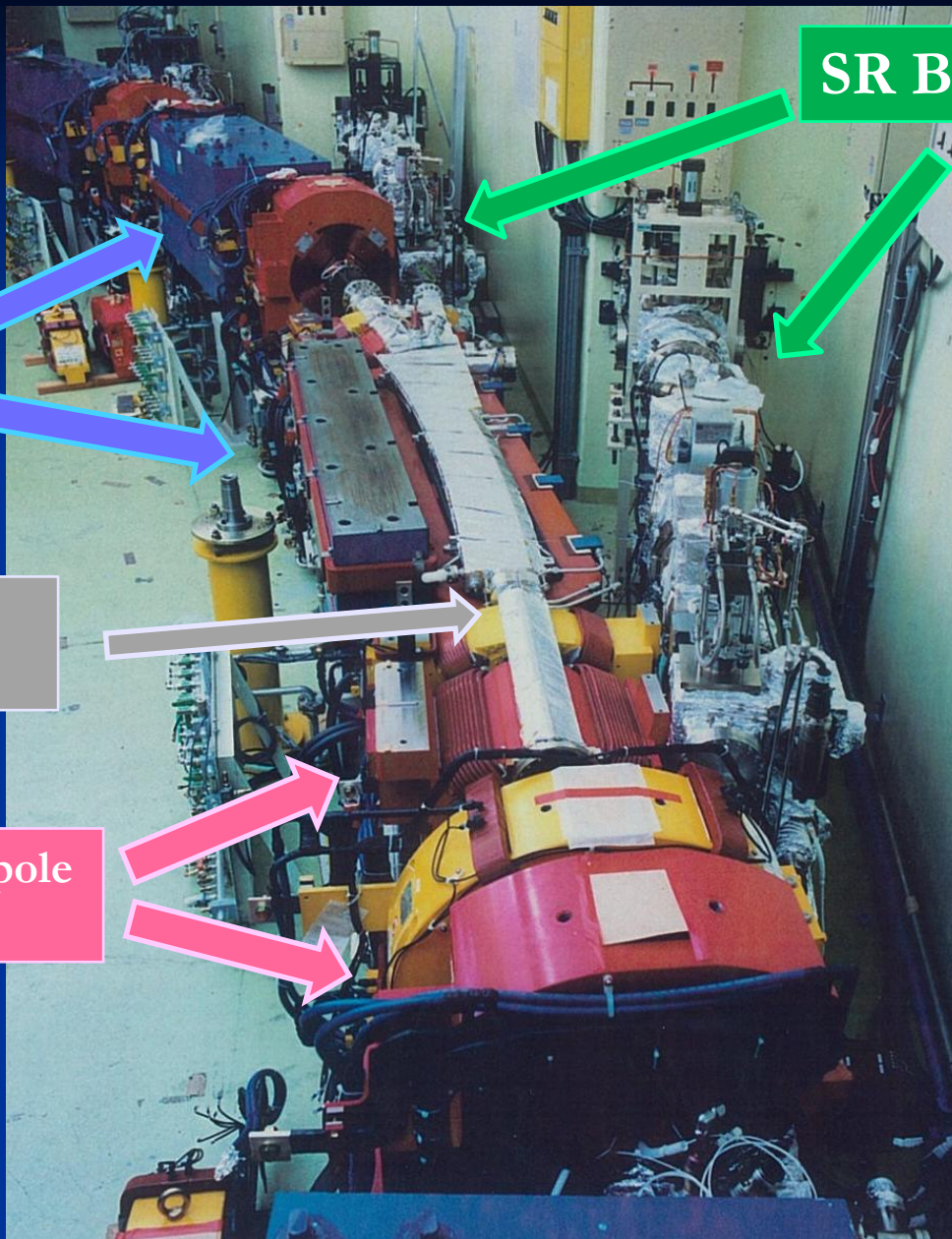
# Electron Storage Ring

Bending Magnet

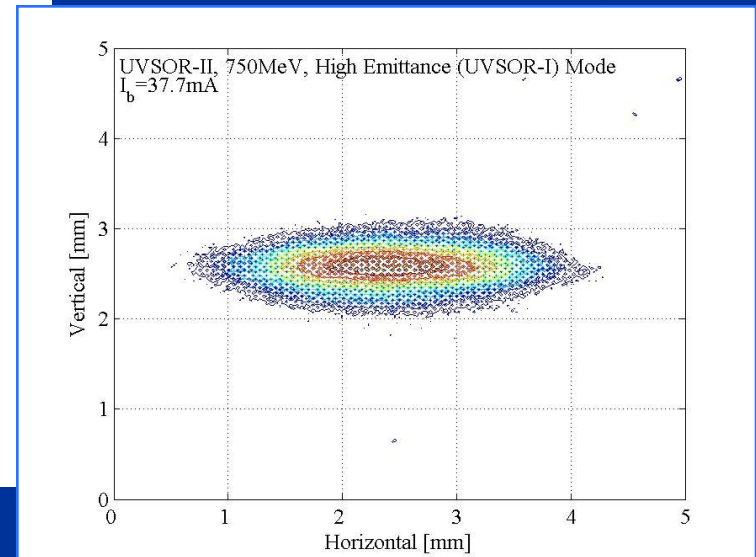
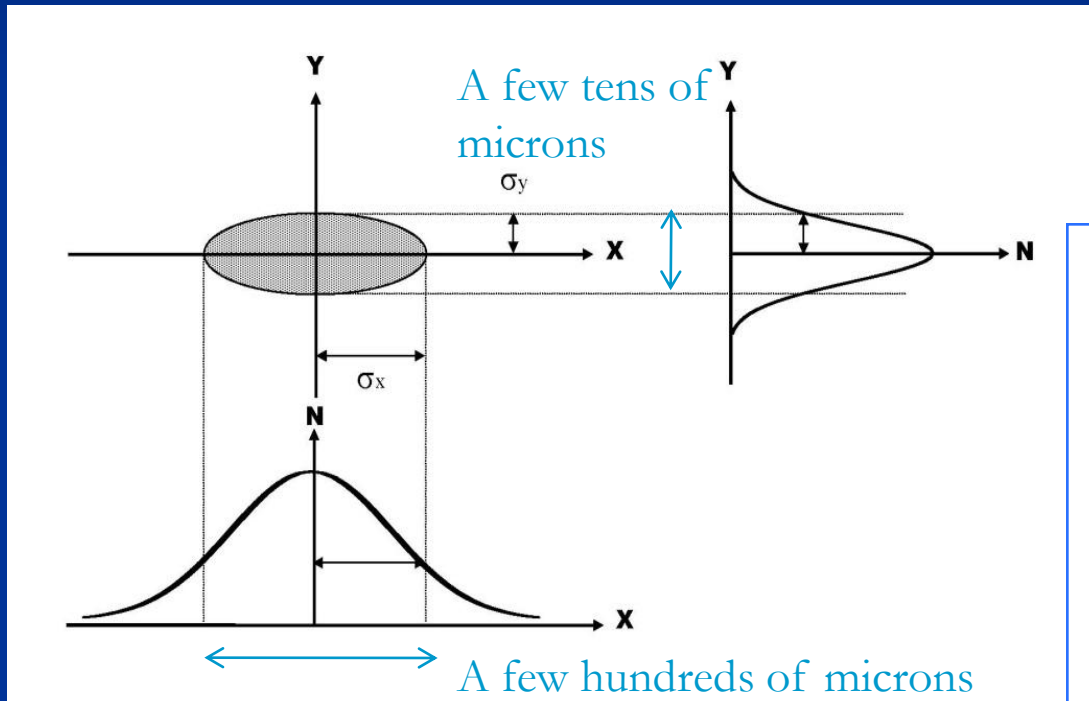
Beam Duct  
(Vacuum Chamber)

Quadrupole Magnet

SR Beam-line

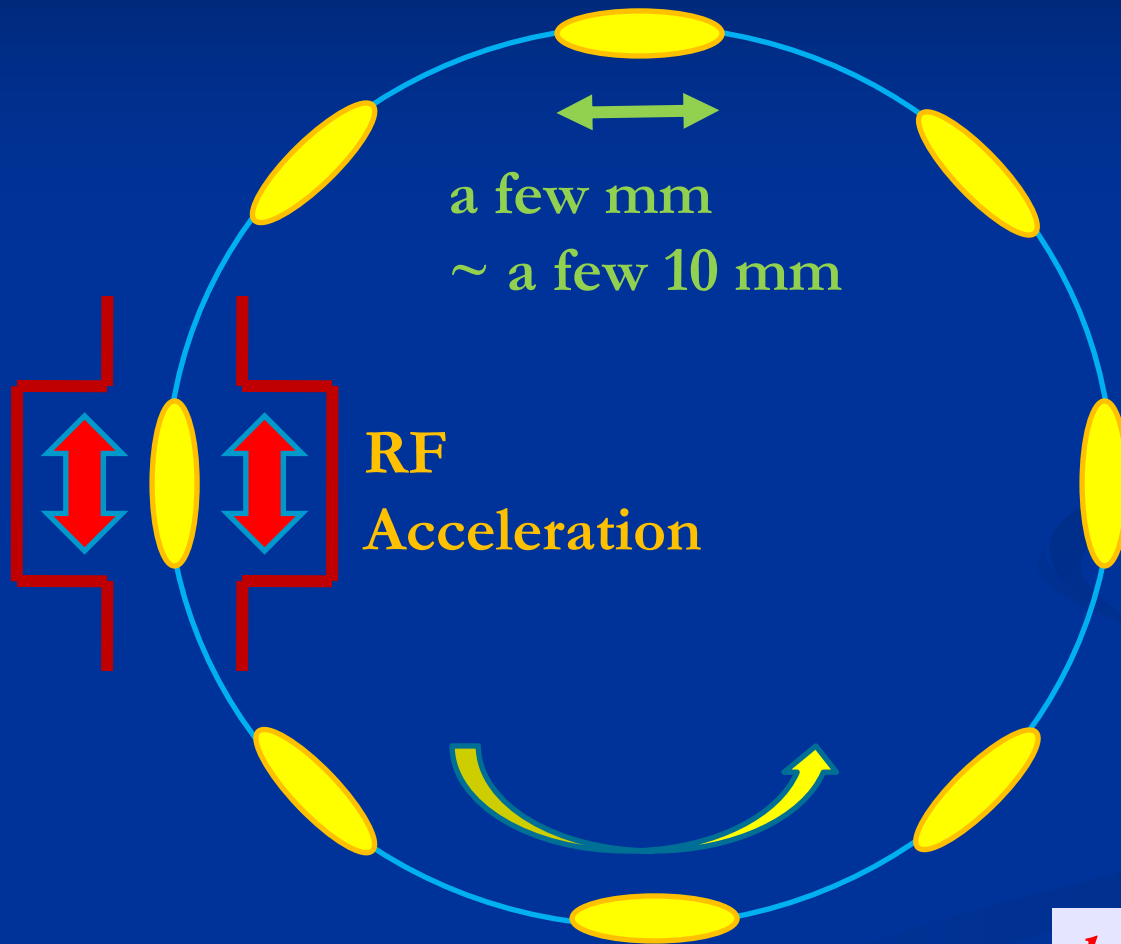


# Transverse Profile of Electron Beam in Storage Rings



Observed cross-section of the electron beam in UVSOR-II

# Bunched Electron Beam



Harmonic Number

$$h = \frac{f_{RF}}{f_{rev}} = \text{integer}$$

UVSOR-II

$$f_{RF} = 90.1 \text{ MHz}$$

$$f_{rev} = 5.6 \text{ MHz}$$

$$h = 16$$

**$h$  = Number of RF buckets**



# Contents

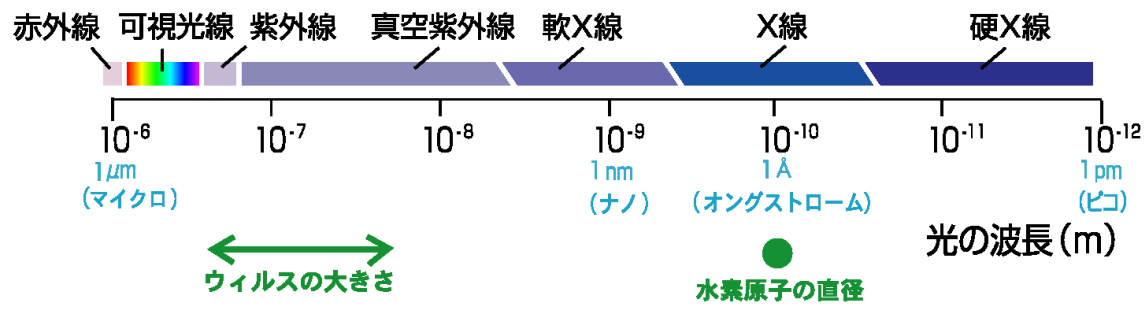
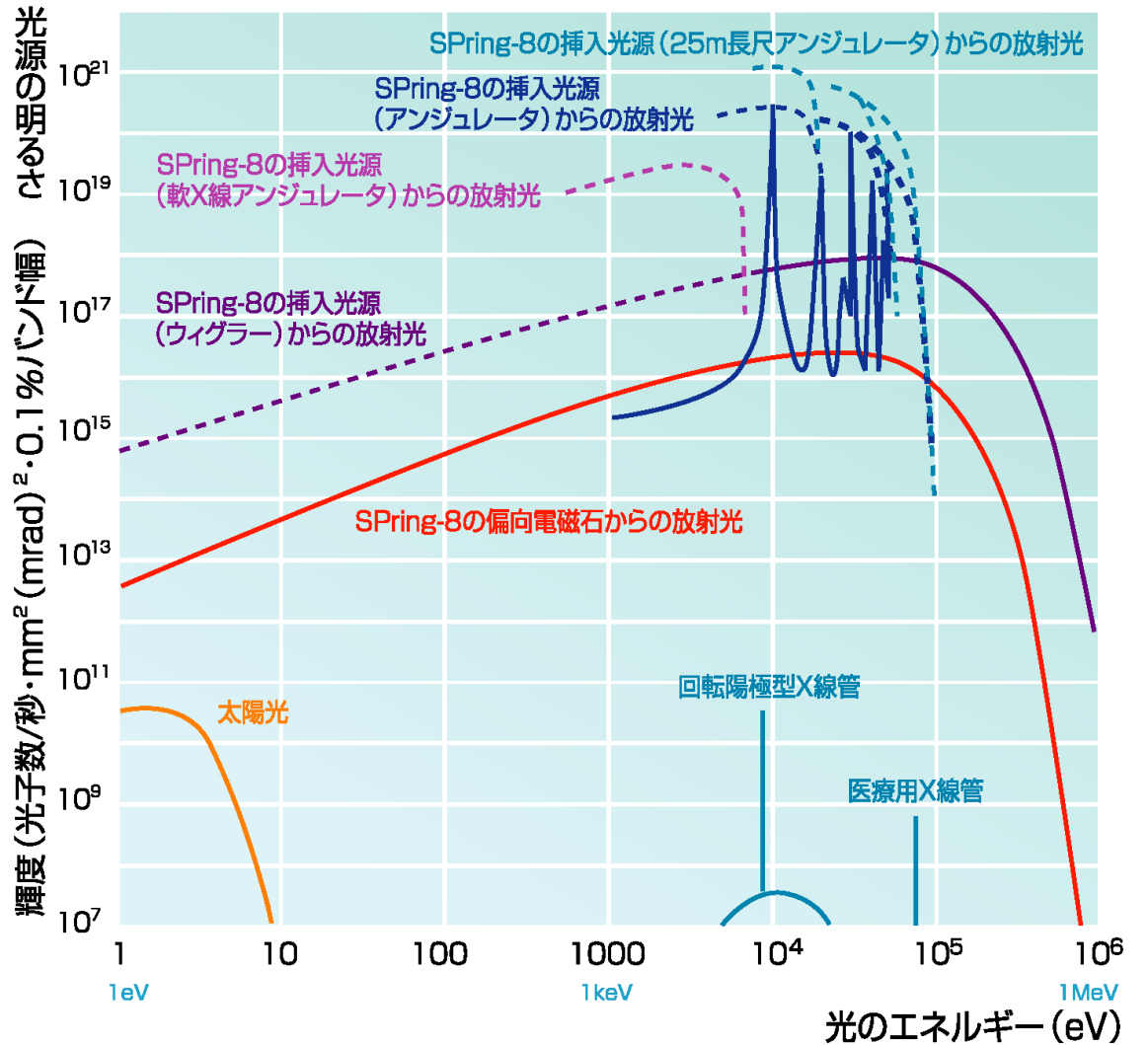
- What is Synchrotron Radiation?
- What is Synchrotron Light Source?
- Characteristics of Synchrotron Radiation
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# Characteristics of Synchrotron Radiation

- Intense
- Collimated
- Broadband
- Polarized
- Pulsed

# Brightness of SR from SPring-8

<http://www.spring8.or.jp/ja/>



# Why intense?

## Larmor Formula for Circular Orbit

$$P = \frac{e^2 c}{6\pi\epsilon_0} \frac{\beta^4}{\rho^2} \gamma^4$$

$$\left( \beta = \frac{v}{c} \approx 1 \right)$$

Lorentz Factor;  $\gamma = E/mc^2$

$$E = 0.75 \text{ GeV} \Rightarrow \gamma \sim 1500$$

$$E = 2.5 \text{ GeV} \Rightarrow \gamma \sim 5000$$

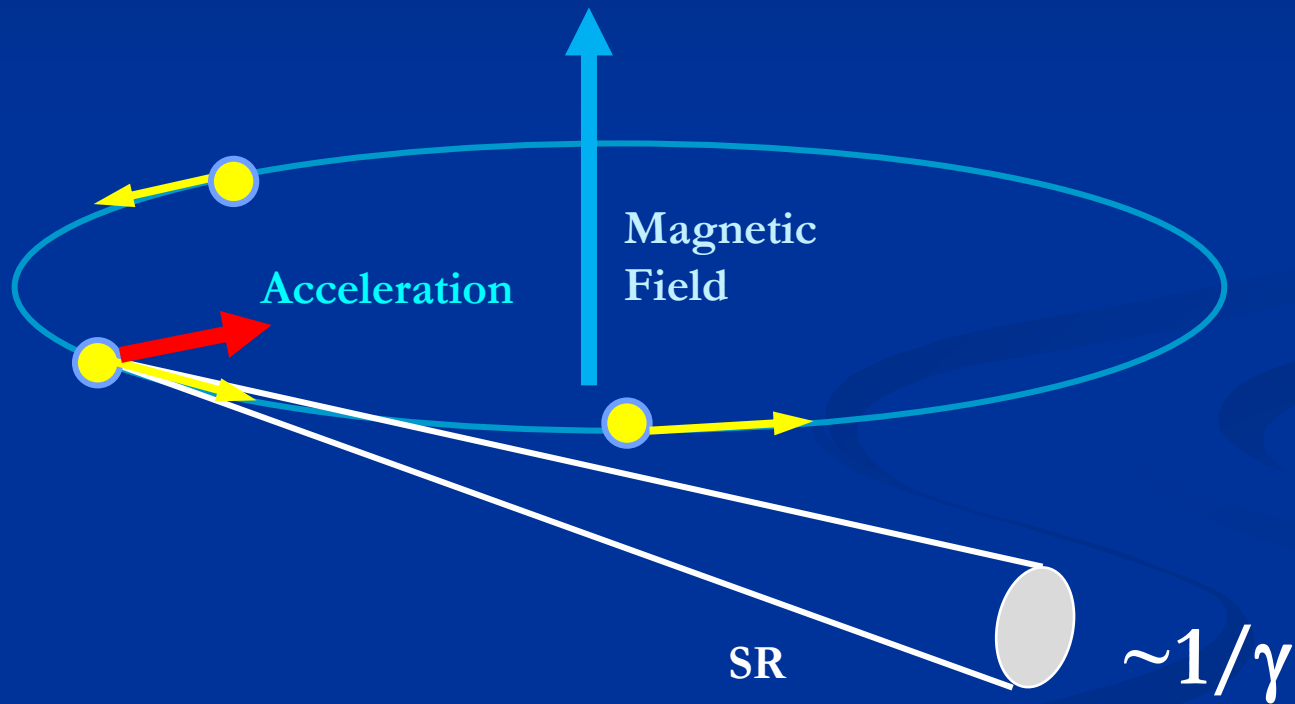
$$E = 8.0 \text{ GeV} \Rightarrow \gamma \sim 16000$$

Example;  $E = 2.5 \text{ GeV}$ ,  $B = 1 \text{ T}$ ,  $\rho = 8.3 \text{ m}$

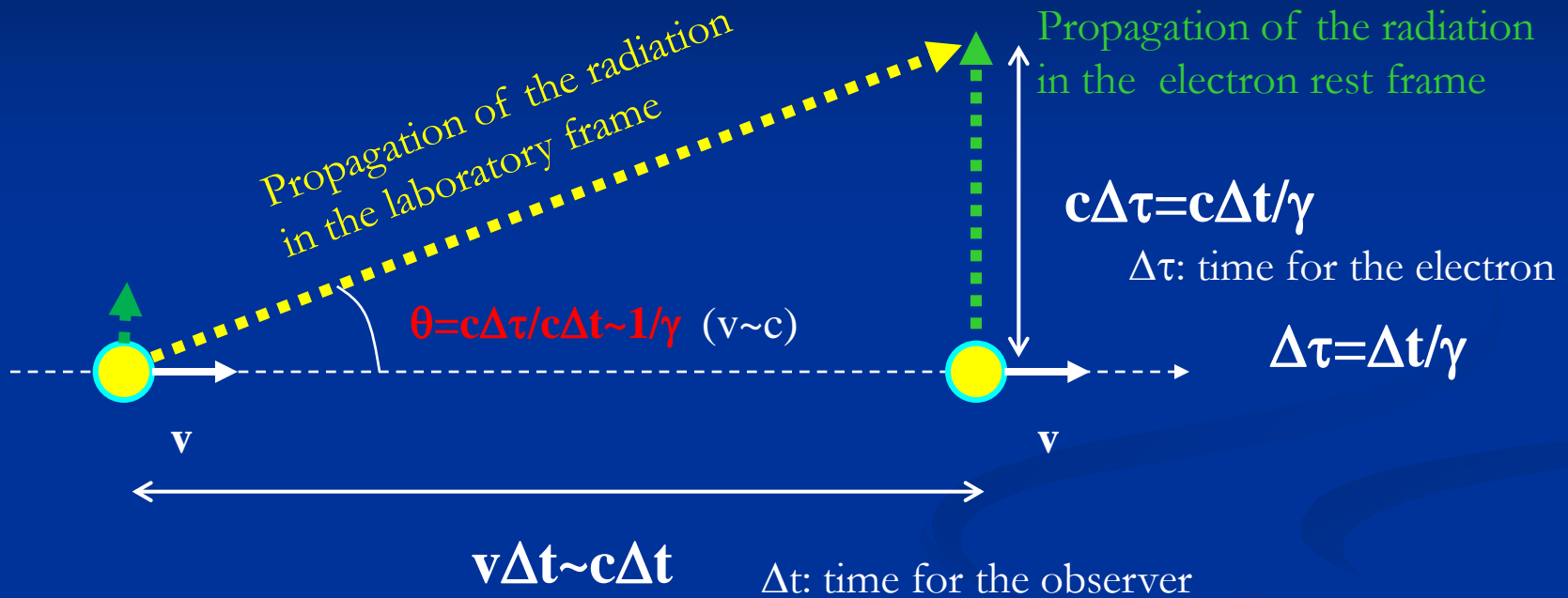
$$\Rightarrow t_d = E/P = \sim 4 \text{ msec}$$

(An electron loses most of its energy within 4 msec.)

# Why collimated?



# Relativistic Beaming



In case of SPring-8 ( $E=8\text{GeV}$ );

$$\gamma \sim 16000$$

$$1/\gamma \sim 1/16000 = 1 \text{ mm} / 16 \text{ m} = 0.06 \text{ mrad}$$

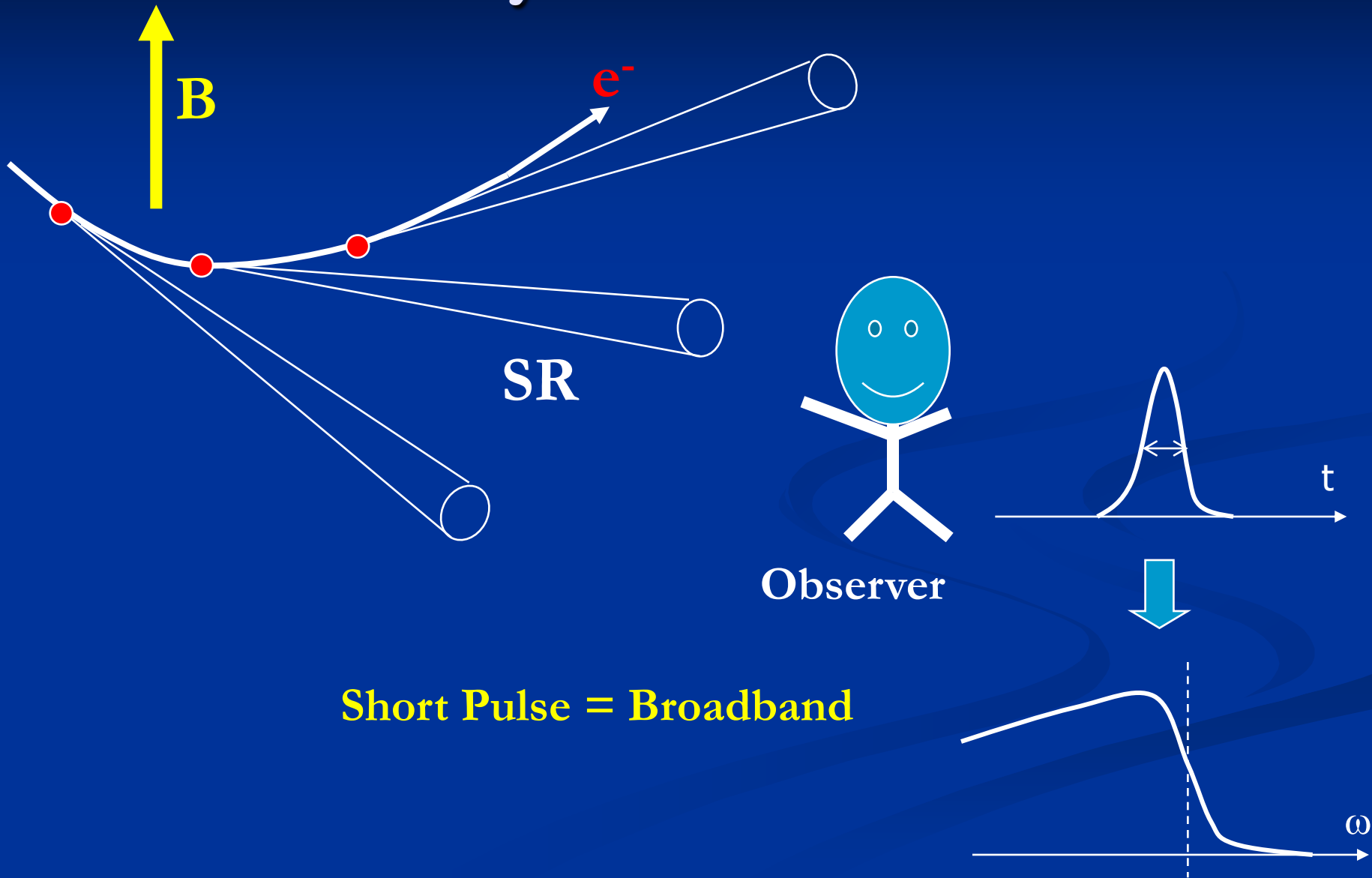
In case of UVSOR-II ( $E=0.75\text{GeV}$ );

$$\gamma \sim 1500$$

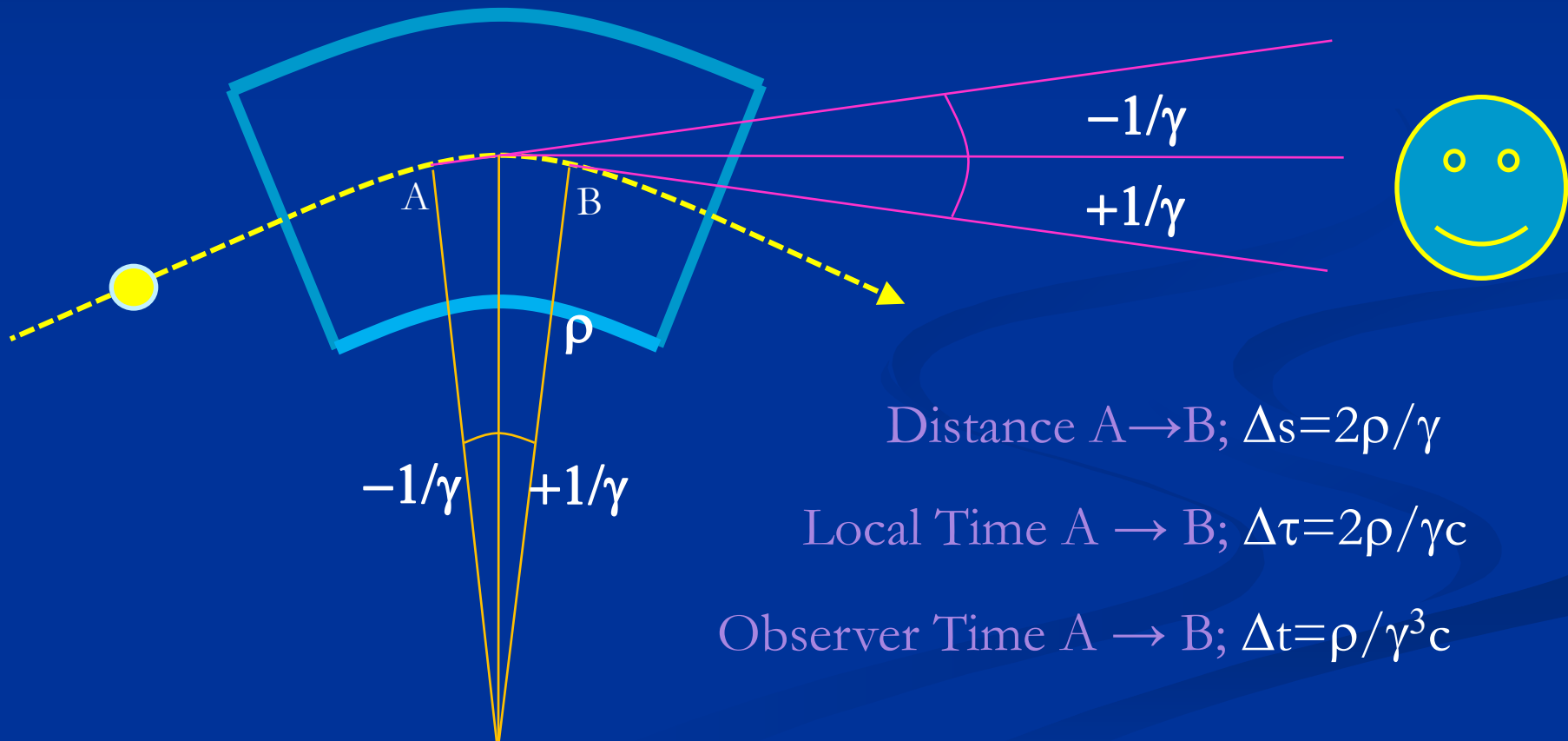
$$1/\gamma \sim 1/1500 = 1 \text{ mm} / 1.5 \text{ m} = 0.7 \text{ mrad}$$



# Why broadband?



# Why broadband? (cont.)

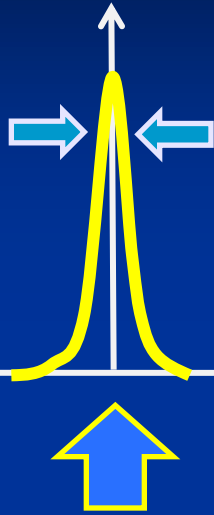


Distance  $A \rightarrow B$ ;  $\Delta s = 2\rho/\gamma$

Local Time  $A \rightarrow B$ ;  $\Delta\tau = 2\rho/\gamma c$

Observer Time  $A \rightarrow B$ ;  $\Delta t = \rho/\gamma^3 c$

# Why broadband? (cont.)



$$\Delta t \approx \frac{\rho}{\gamma^3 c}$$

A short pulse contains frequency components in wide range.

The highest frequency is given by

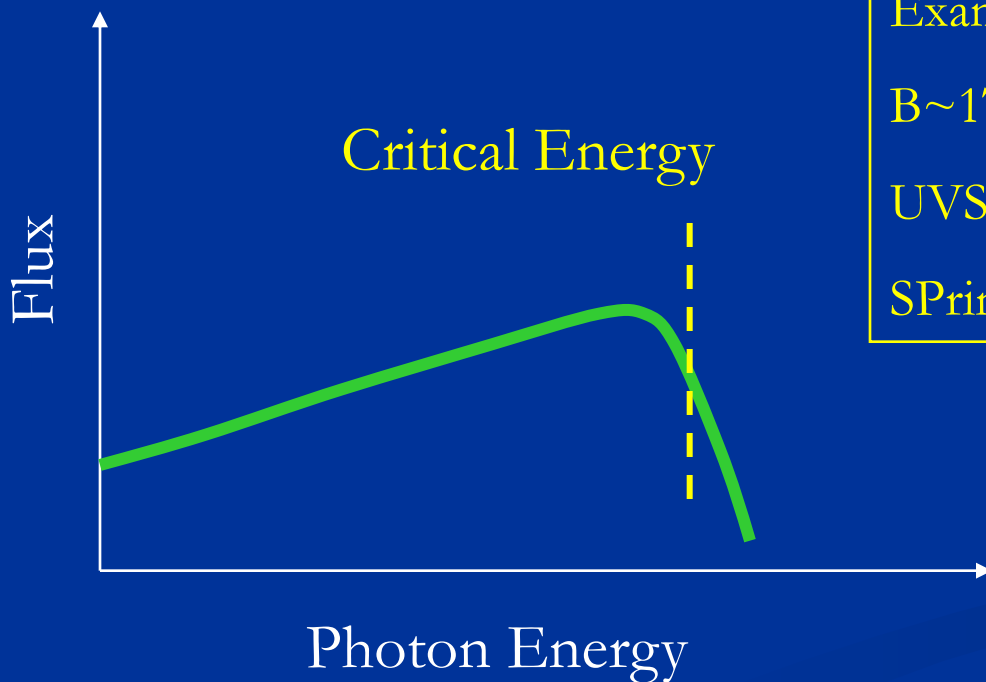
$$\omega_c \approx \frac{1}{\Delta t}$$

In case of UVSOR-II,  $\rho \sim 2$  m,  
 $c = 3 \times 10^8$  m/s,  $\gamma \sim 1500$

$\Rightarrow \Delta t \sim 10^{-18}$  s,  $\epsilon_c = h/2\pi\omega_c \sim 600$  eV

# Critical Energy of Synchrotron Radiation

$$h\nu_c [keV] = 0.665 E_e^2 [GeV] B [T]$$



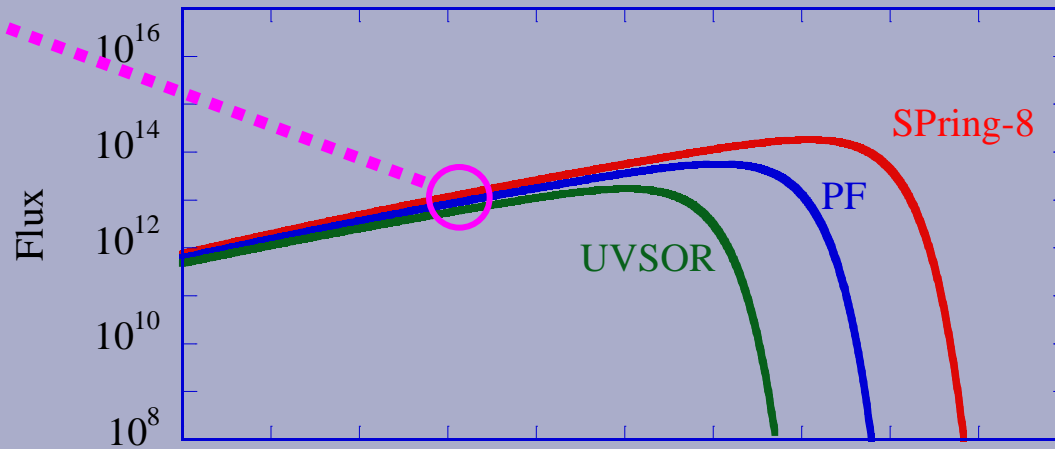
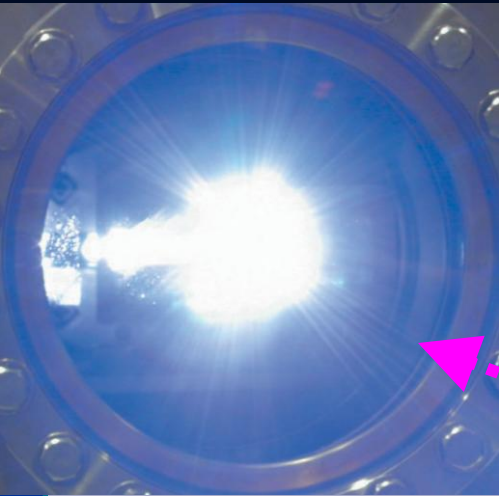
Example;

$B \sim 1T$  for normal conducting magnets.

UVSOR-II;  $E_e = 0.75 \text{ GeV} \Rightarrow \epsilon_c \sim 0.4 \text{ keV}$

SPring-8;  $E_e = 8.0 \text{ GeV} \Rightarrow \epsilon_c \sim 40 \text{ keV}$

# Extremely Broadband from millimeter wave to X-rays



1m

1mm

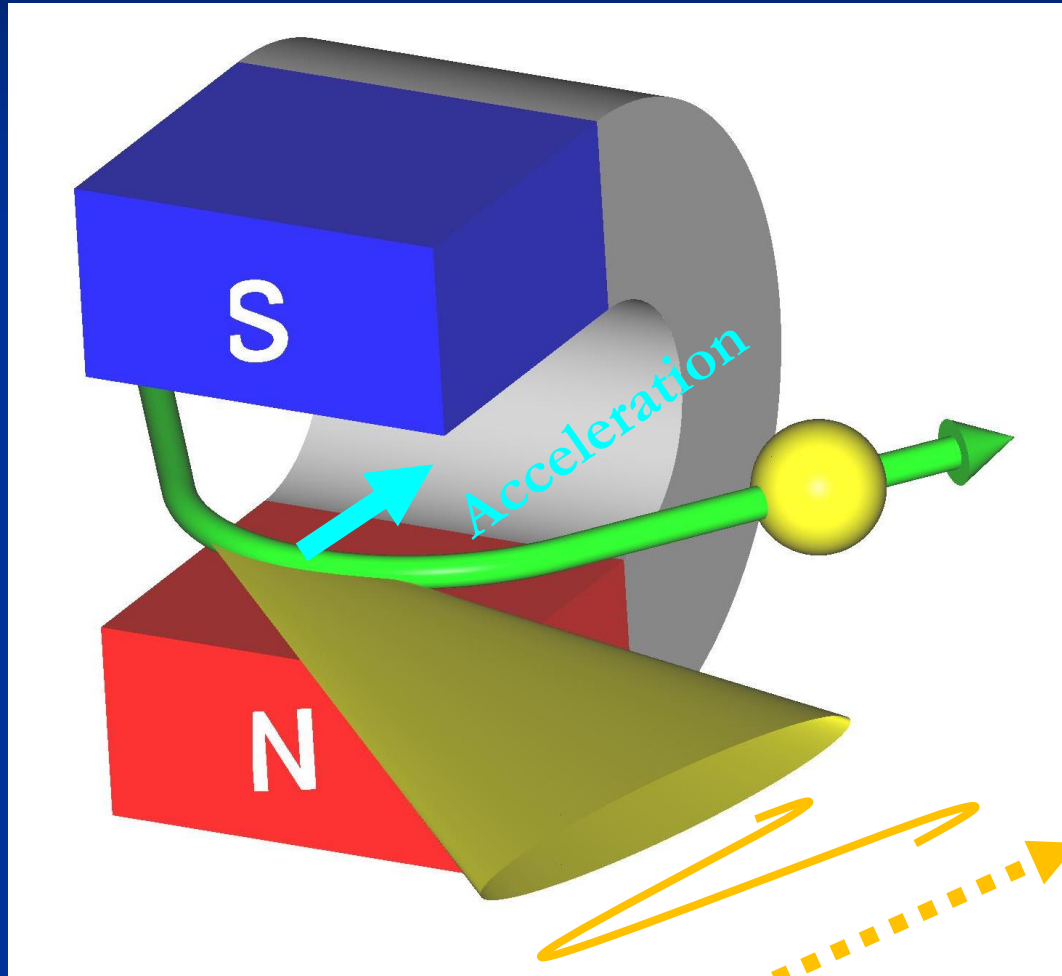
1 $\mu$ m

1nm

1pm

Wavelength

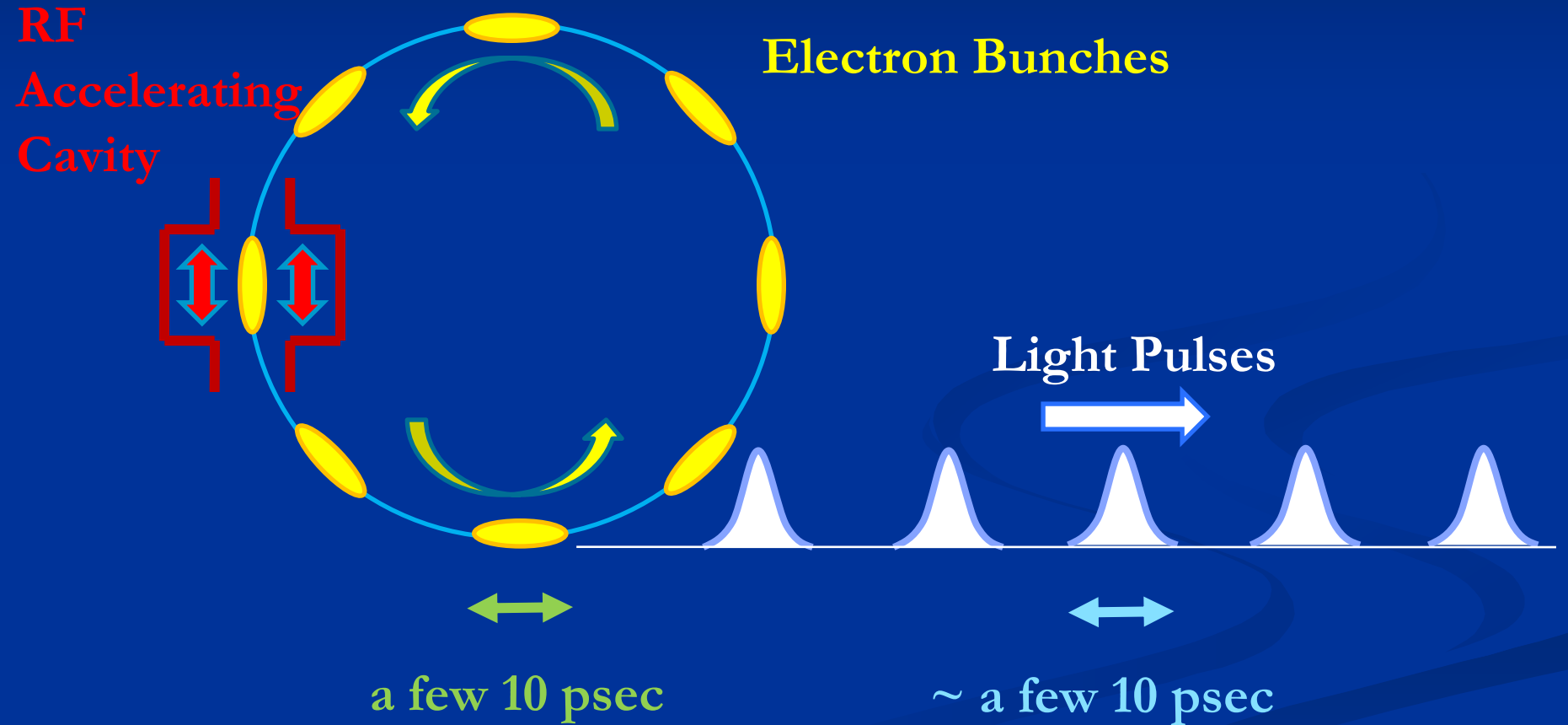
# Why highly polarized?



Electric Field

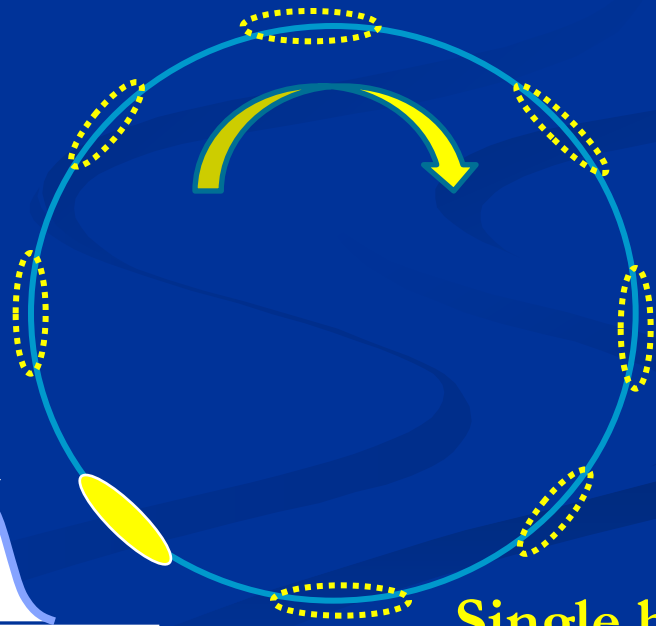
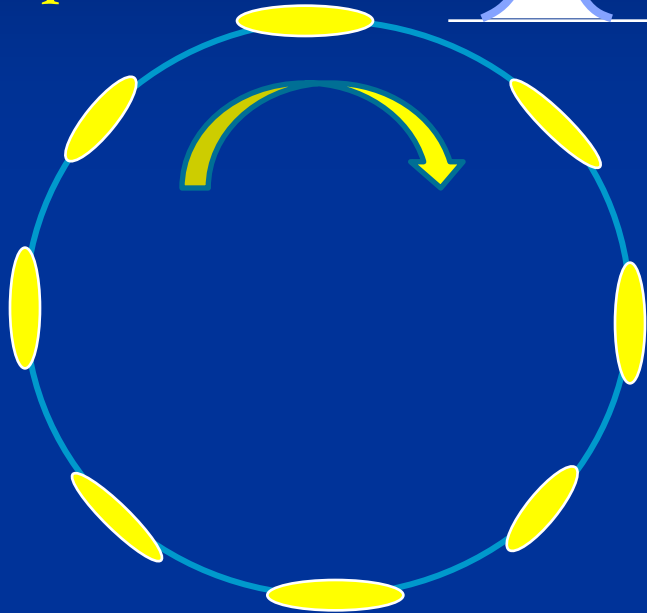
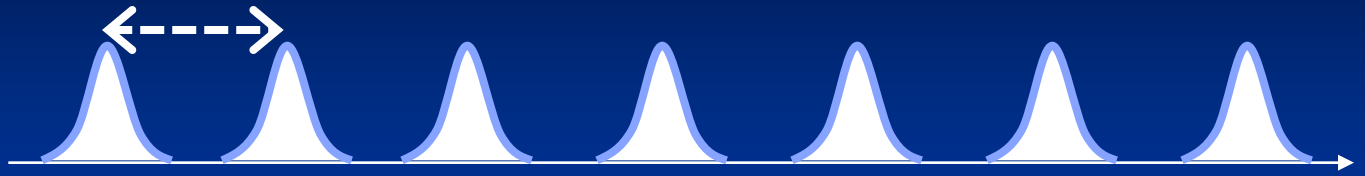


# Why pulsed?



# Time Structure of SR

Multi-bunch  
Operation



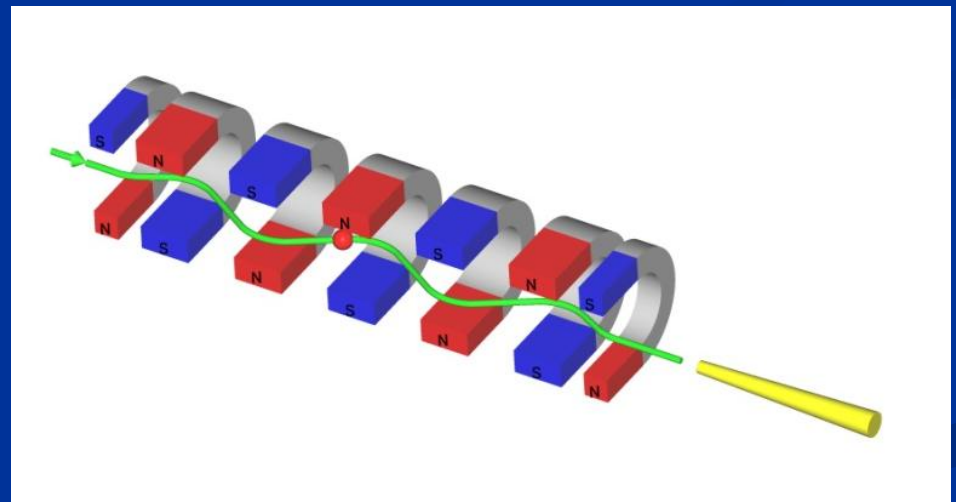
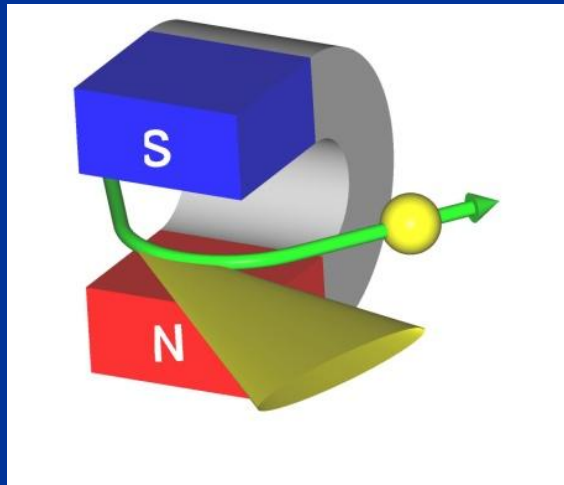
Single bunch  
Operation

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# Towards Higher Brightness

Bending Magnet  $\Rightarrow$  Undulator



# Undulator

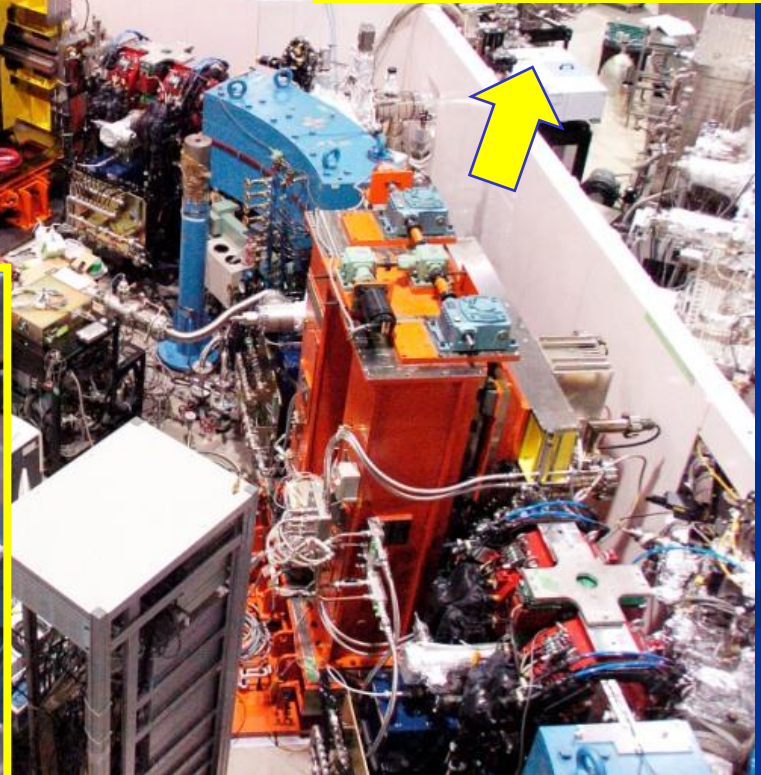
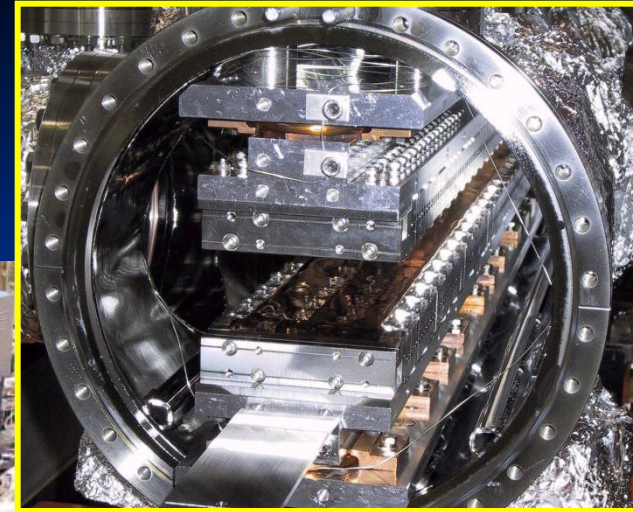


Configuration	APPLE-II
Polarization	Hor/Ver/Helical
Number of periods	40
Period length	76 mm
Total Length	3040 mm
Remanent field	1.3 T
Magnetic gap	24 – 200 mm
Deflection parameter (K)	
(horizontal mode)	max. 5.4
(vertical mode)	max. 3.6
(helical mode)	max. 3.0

Variable Polarization Undulator at UVSOR-II BL7U  
Institute for Molecular Science, Okazaki, Japan

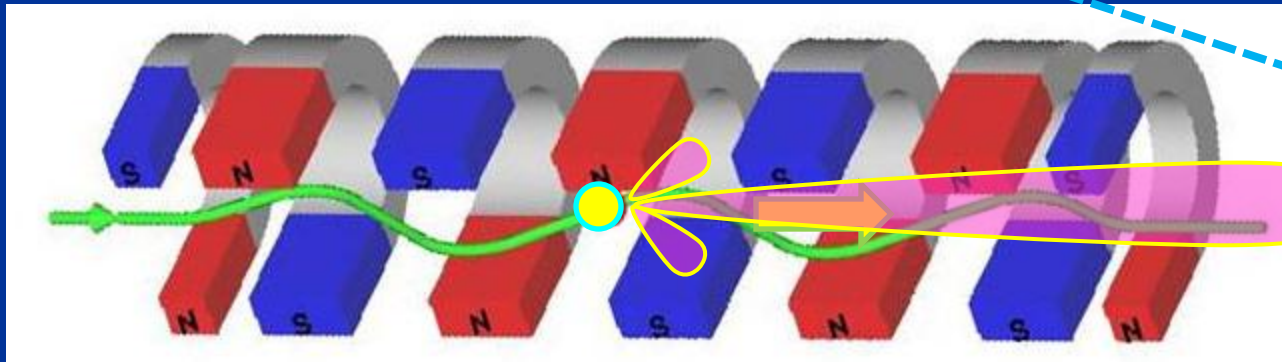
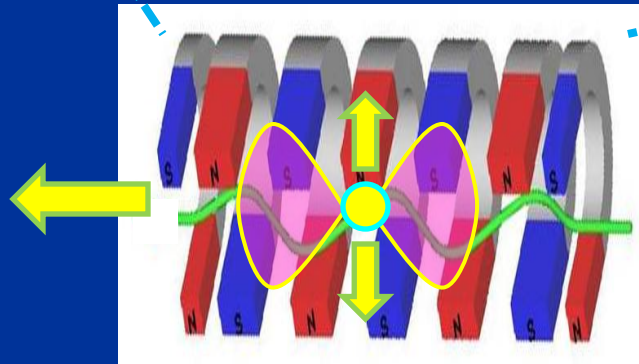
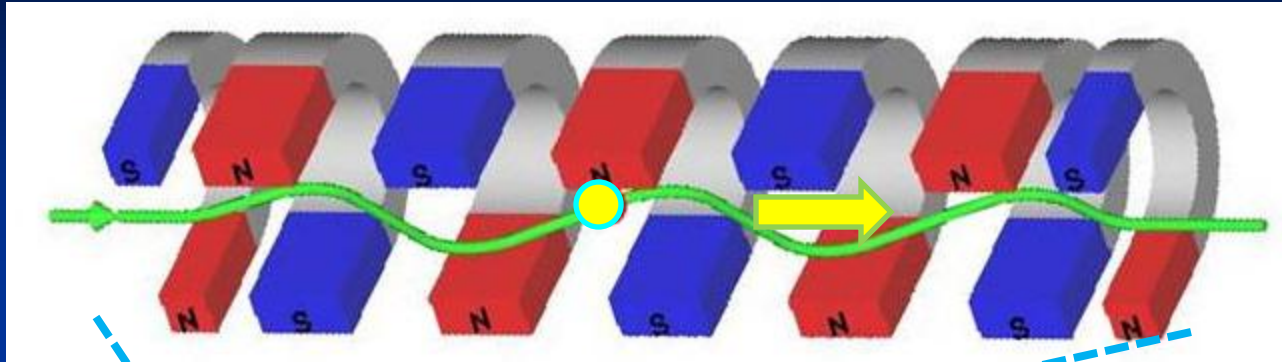


**UNSOR II**  
since 2003





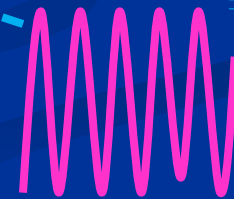
# Principle of Undulator



Lorentz Contraction



Doppler Effect



# Undulator Radiation Spectrum (cont.)

$$h\nu[\text{keV}] = \frac{0.95E_e^2[\text{GeV}]}{(1 + K^2/2)\lambda_u[\text{cm}]}$$

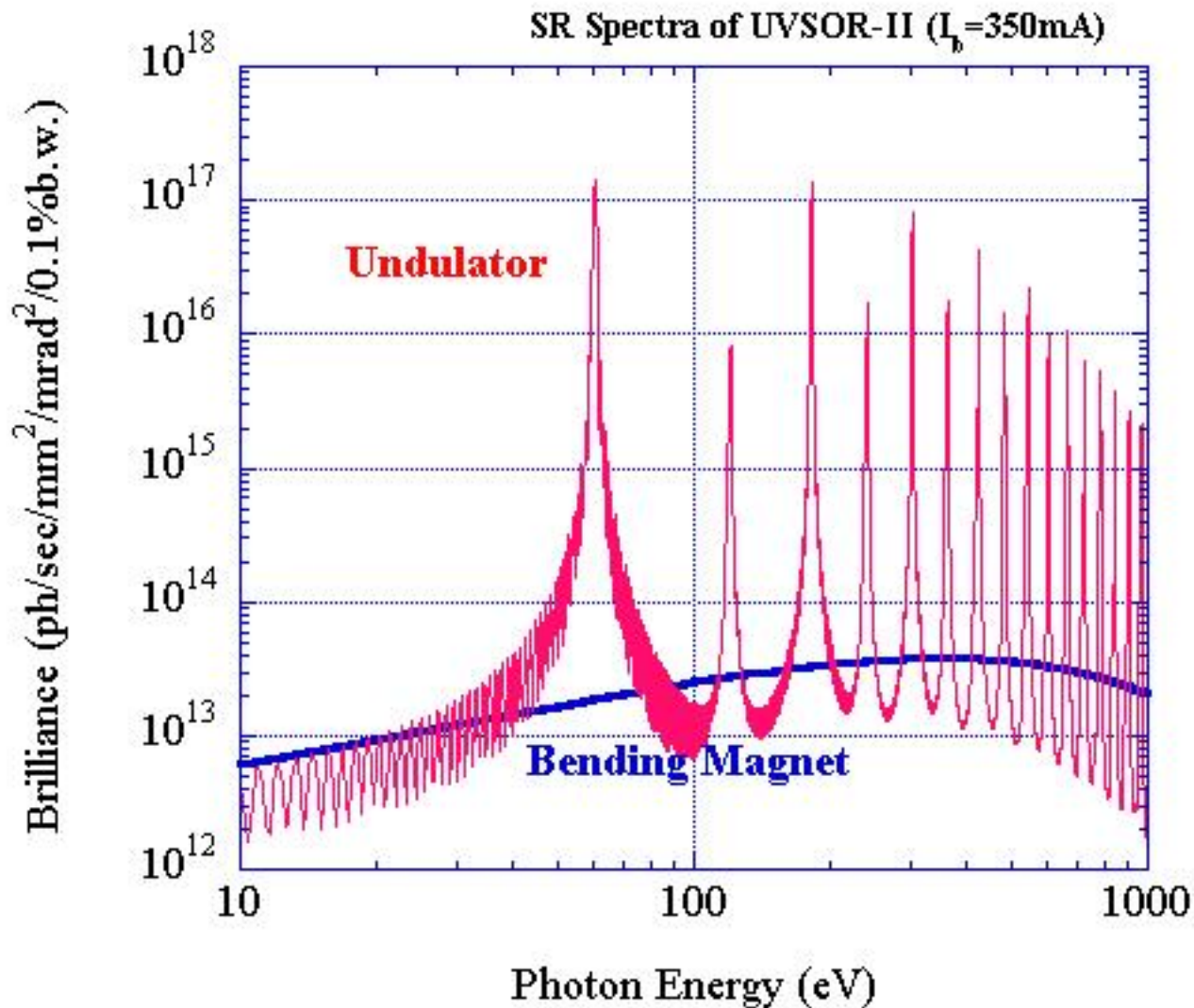
$$K = 0.934\lambda_u[\text{cm}]B_0[\text{T}]$$

Example;

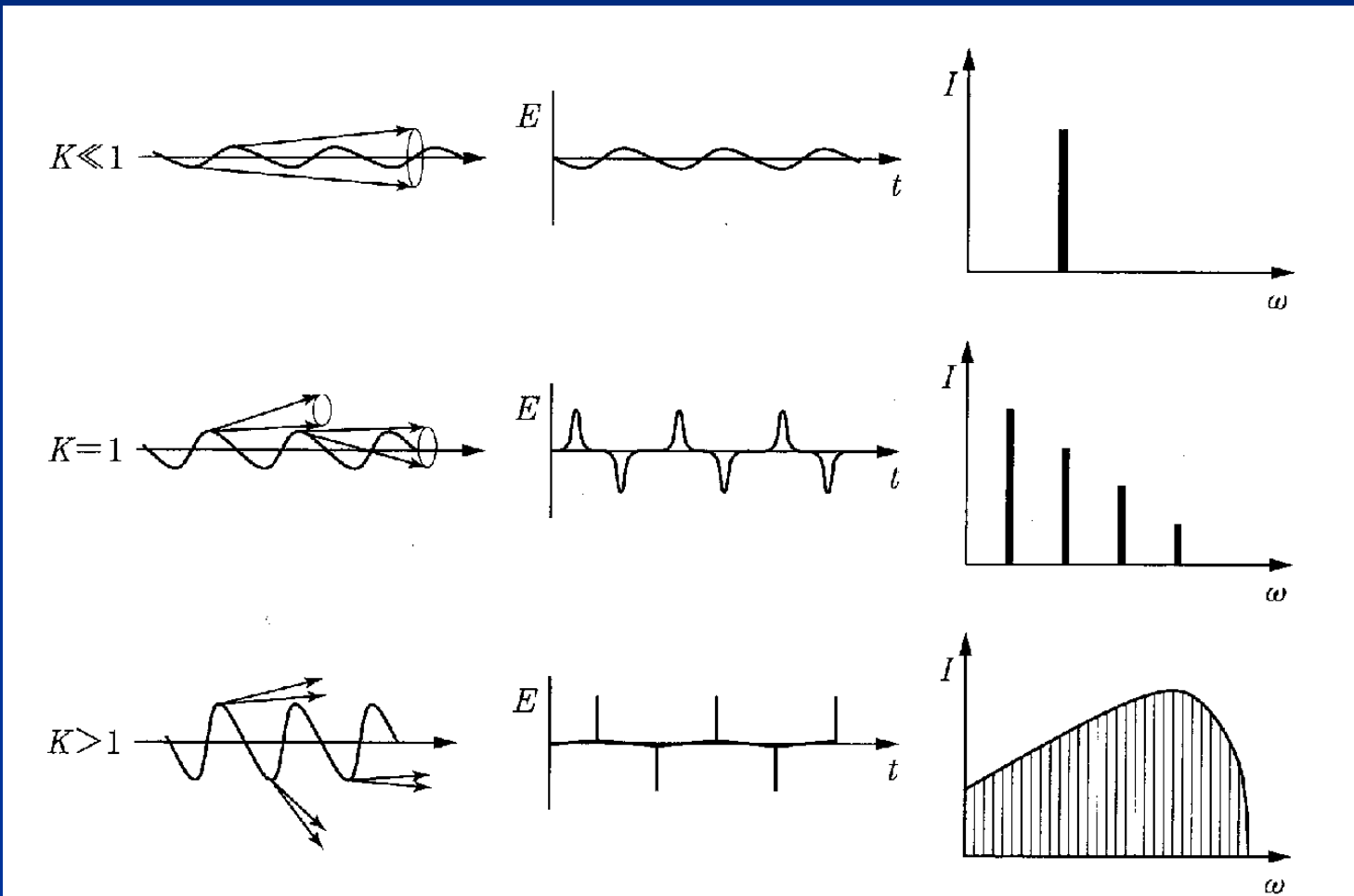
$$E_e = 8 [\text{GeV}], \lambda_u = 3.2 [\text{cm}], B_0 = 0.5 [\text{T}]$$

$$\Rightarrow h\nu \sim 9 [\text{keV}]$$

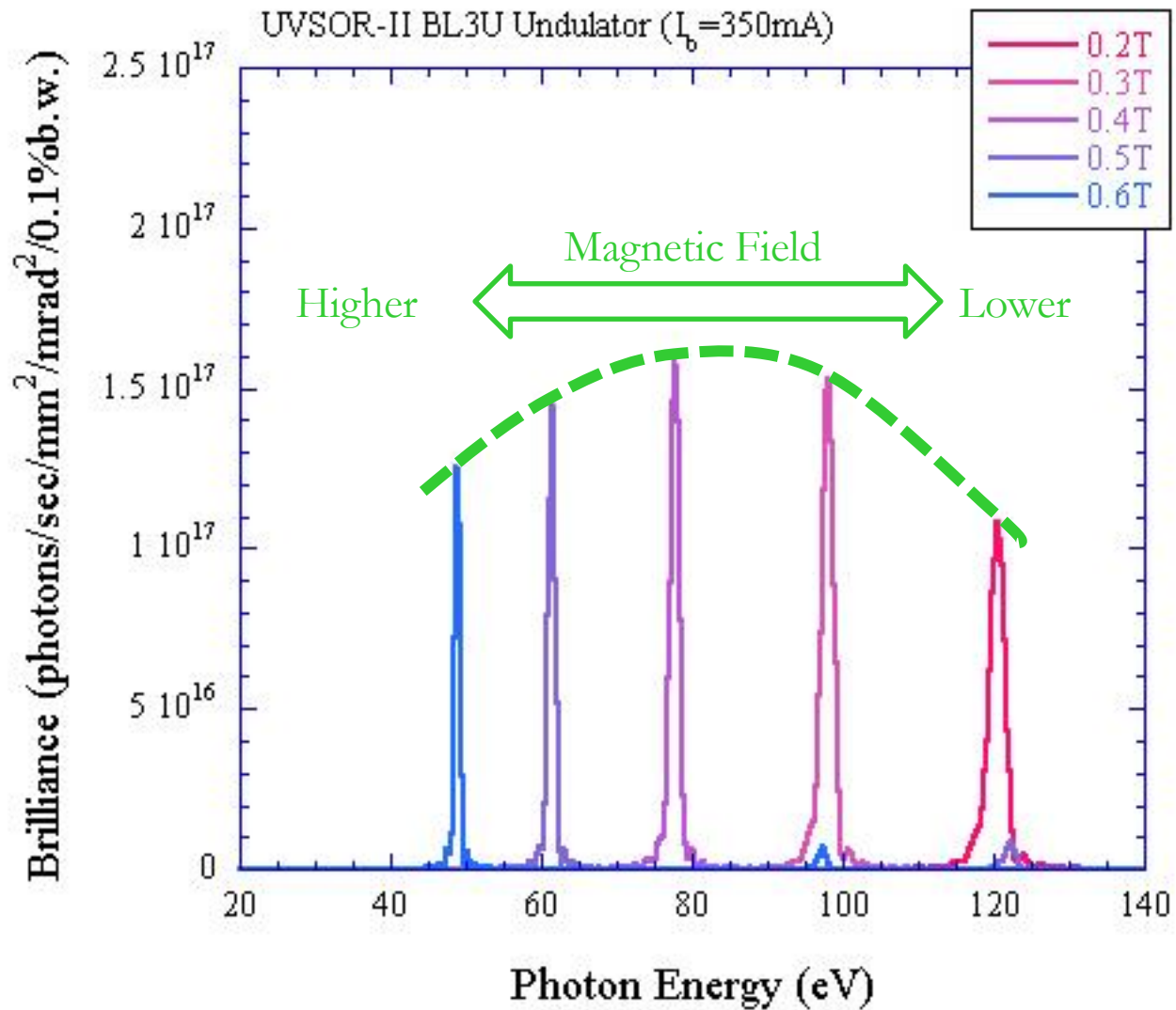
# Undulator Radiation Spectrum (cont.)



# Why Higher Harmonics?



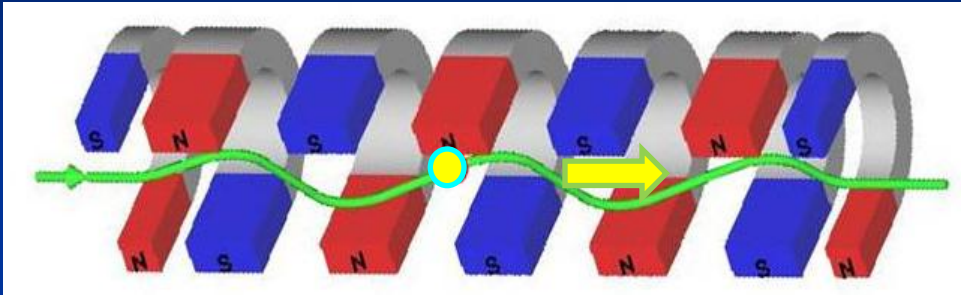
# Tunability





# Why Tunable?

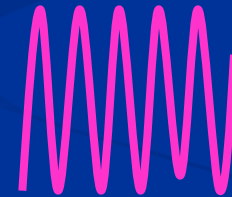
Average Velocity of Electron in Undulator



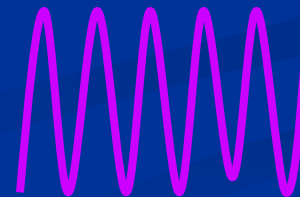
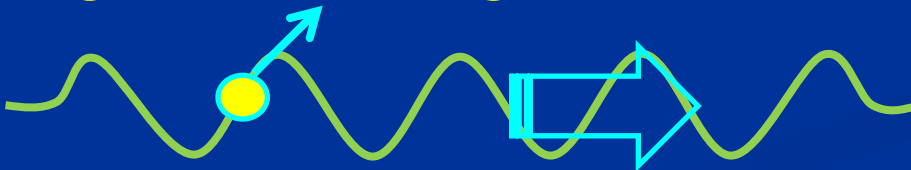
$$\bar{v}_z = v \left( 1 - \frac{K^2}{4\gamma^2} \right)$$

$$K = \frac{eB_0\lambda_u}{2\pi mc}$$

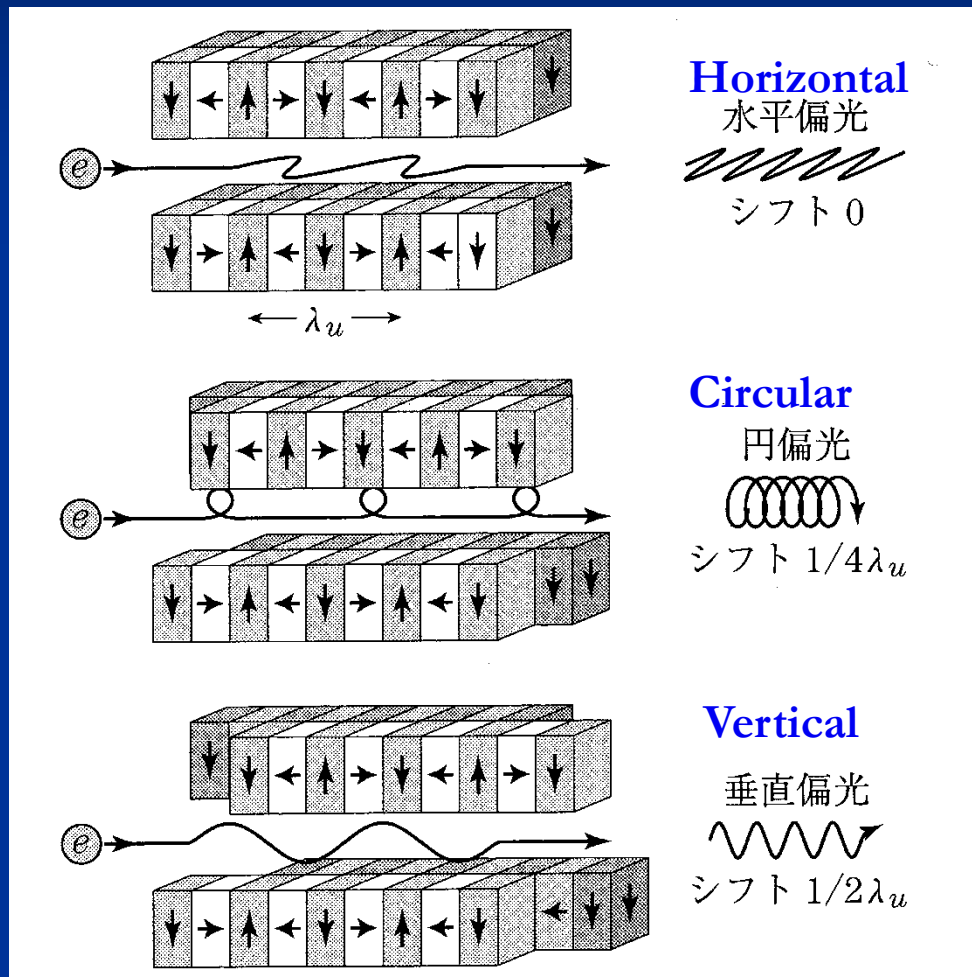
Small K; Electrons go fast.



Large K; Electrons go slow.



# Variable Polarization Undulator

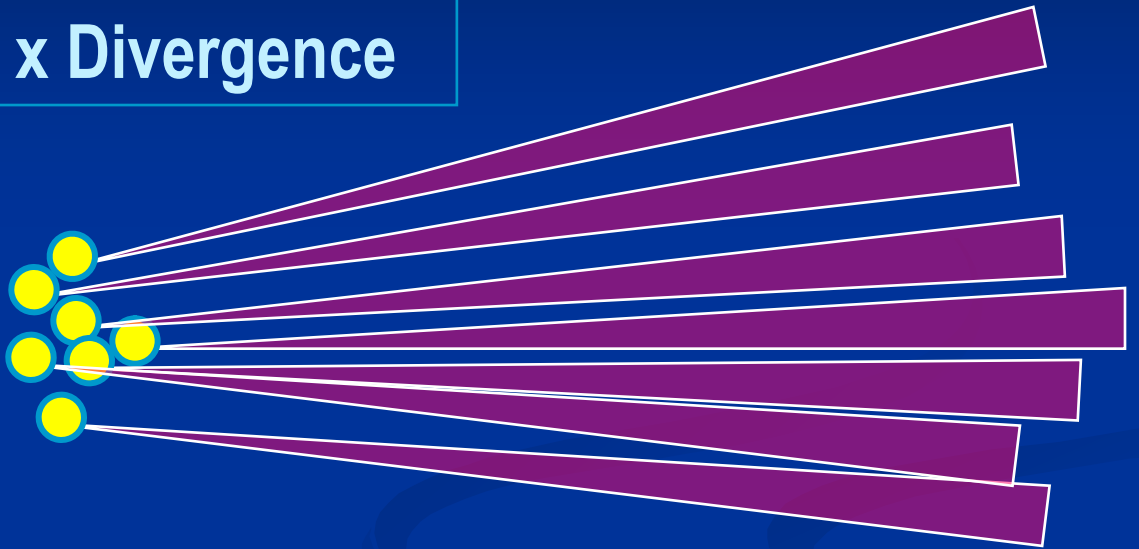


S. Sasaki, NIM A347 (1994) 83

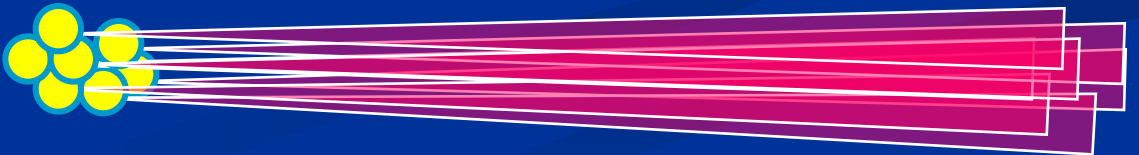
# Towards Higher Brightness Low Emittance Electron Beam

Emittance = Size x Divergence

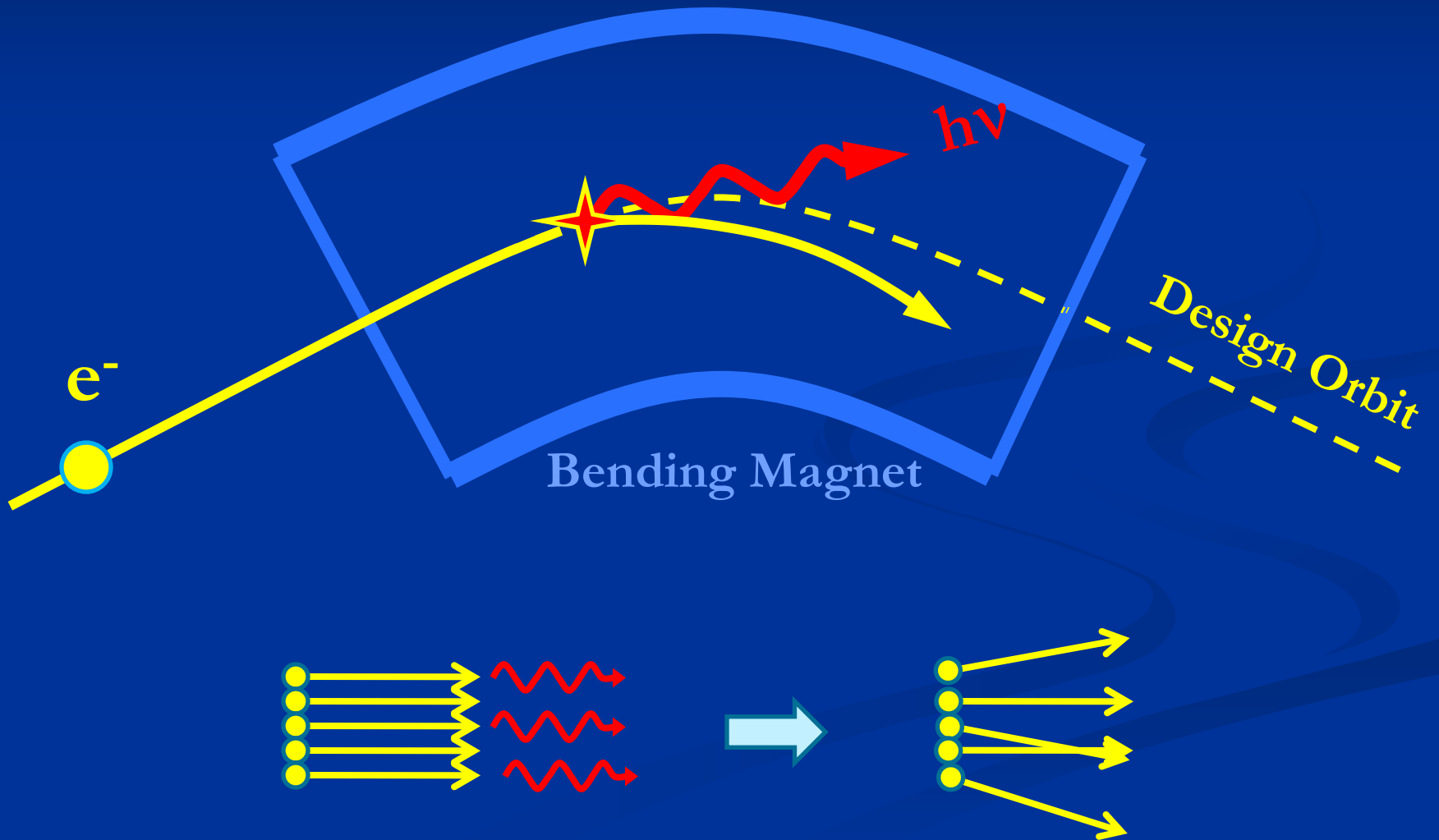
High emittance  
electron beam



Low emittance  
electron beam

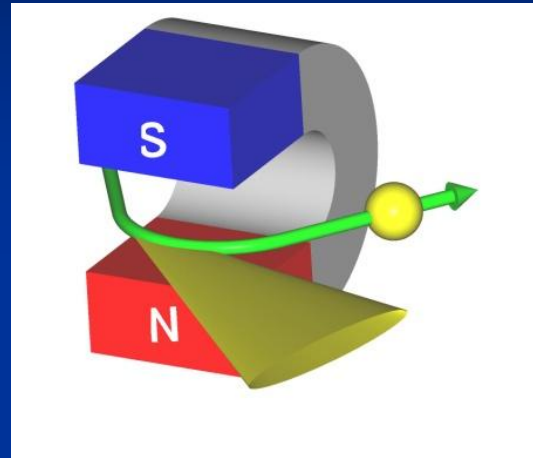


# Radiation Excitation

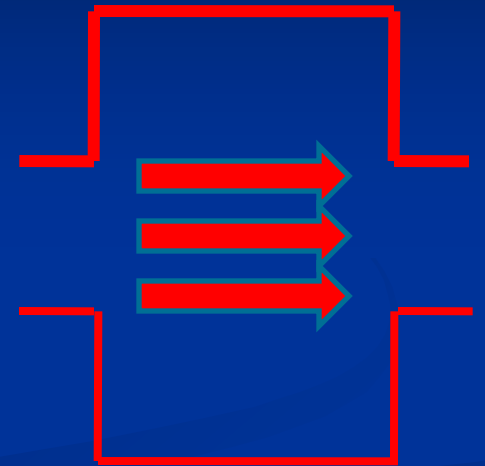


# Radiation Damping

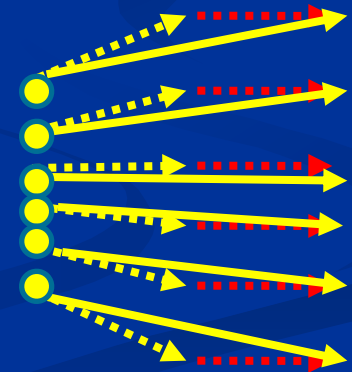
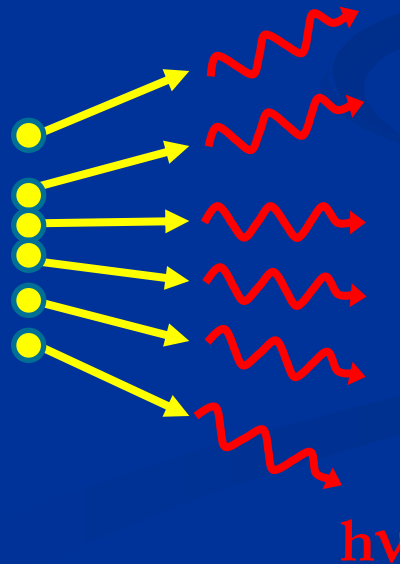
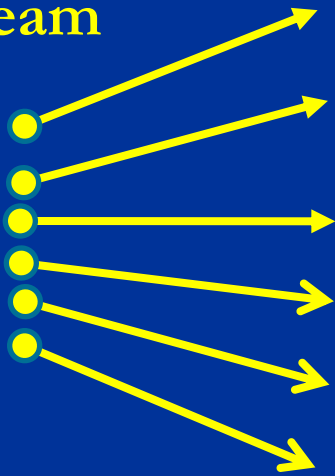
Bending Magnet



Accelerating Cavity

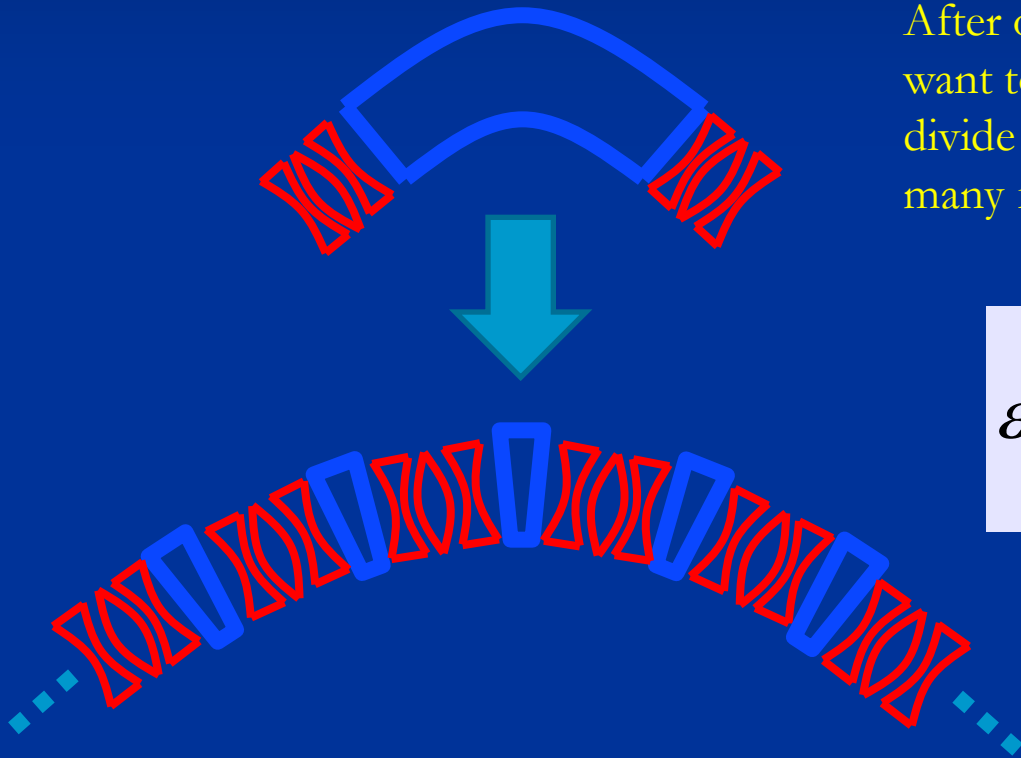


e-beam





# Low Emittance Lattice



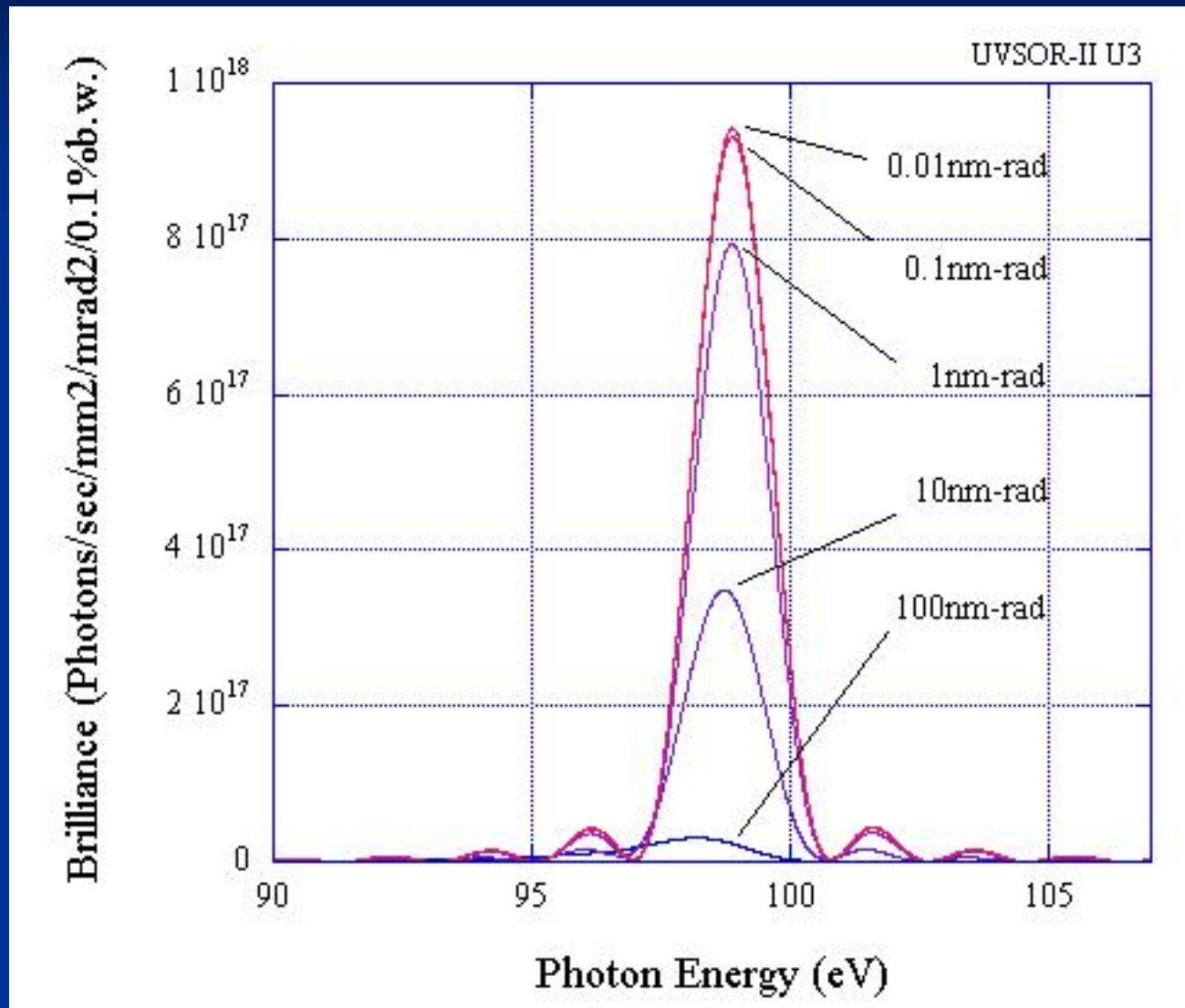
After optimizing the focusing magnets, if we want to reduce the emittance more, we must divide bending magnets in small peaces and put many focusing magnets between them.

$$\varepsilon = F(\nu_x, \text{lattice}) \frac{E^2 [\text{GeV}]}{J_x N_d^3}$$

$N_d$ ; Number of Bending Magnets

J. B. Murphy, BNL 42333 (1996)

# Diffraction Limit on Brilliance



# Effect of Emittance on Brilliance

## Brilliance of Undulator Radiation

$$B = \frac{F}{(2\pi)^2 \Sigma_x \Sigma_{x'} \Sigma_y \Sigma_{y'}}$$

Flux into the central cone

$$F = \frac{\pi}{2} \alpha N \frac{\Delta\omega}{\omega} \frac{I}{e} Q_n(K)$$

Effective Source Size and Divergence

$$\Sigma_x = \sqrt{\sigma_r^2 + \sigma_x^2}$$

$$\Sigma_{x'} = \sqrt{\sigma_{r'}^2 + \sigma_{x'}^2}$$

$$\Sigma_y = \sqrt{\sigma_r^2 + \sigma_y^2}$$

$$\Sigma_{y'} = \sqrt{\sigma_{r'}^2 + \sigma_{y'}^2}$$

Size and Divergence of e-Beam

$$\varepsilon_x = \sigma_x \sigma_{x'}$$

$$\varepsilon_y = \sigma_y \sigma_{y'}$$

Size and Divergence of Undulator Radiation

$$\sigma_r = \sqrt{2\lambda L} / 4\pi$$

$$\sigma_{r'} = \sqrt{\lambda / 2L}$$

$$\varepsilon_r = \sigma_r \sigma_{r'} = \frac{\lambda}{4\pi}$$

# Diffraction Limit

$$B = \frac{F}{(2\pi)^2 \sum_x \sum_{x'} \sum_y \sum_{y'}}$$

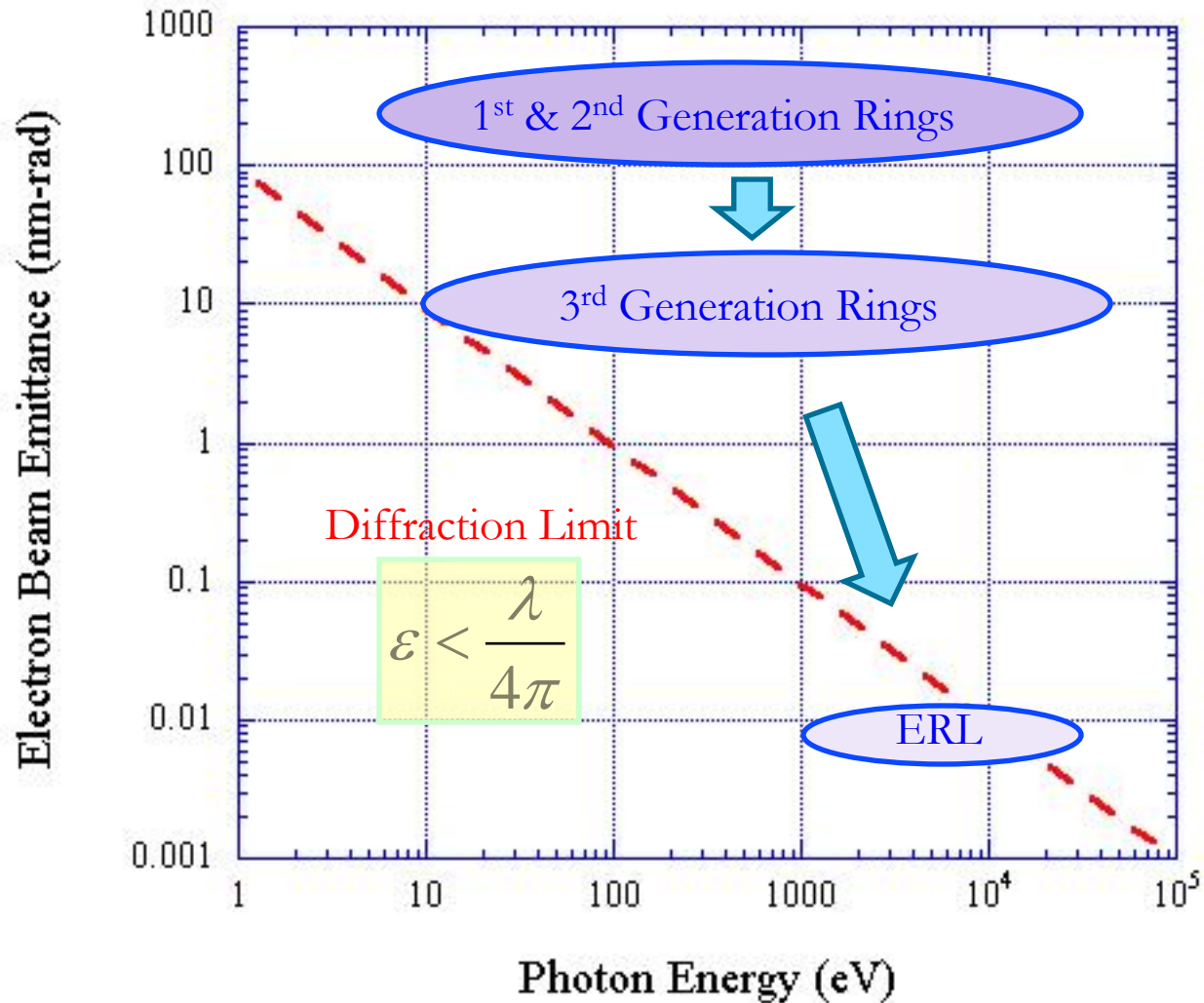


$$\begin{aligned} \sigma_x, \sigma_y &\ll \sigma_r \\ \sigma_{x'}, \sigma_{y'} &\ll \sigma_{r'} \end{aligned}$$

$$\varepsilon_r = \sigma_r \sigma_{r'} = \frac{\lambda}{4\pi}$$

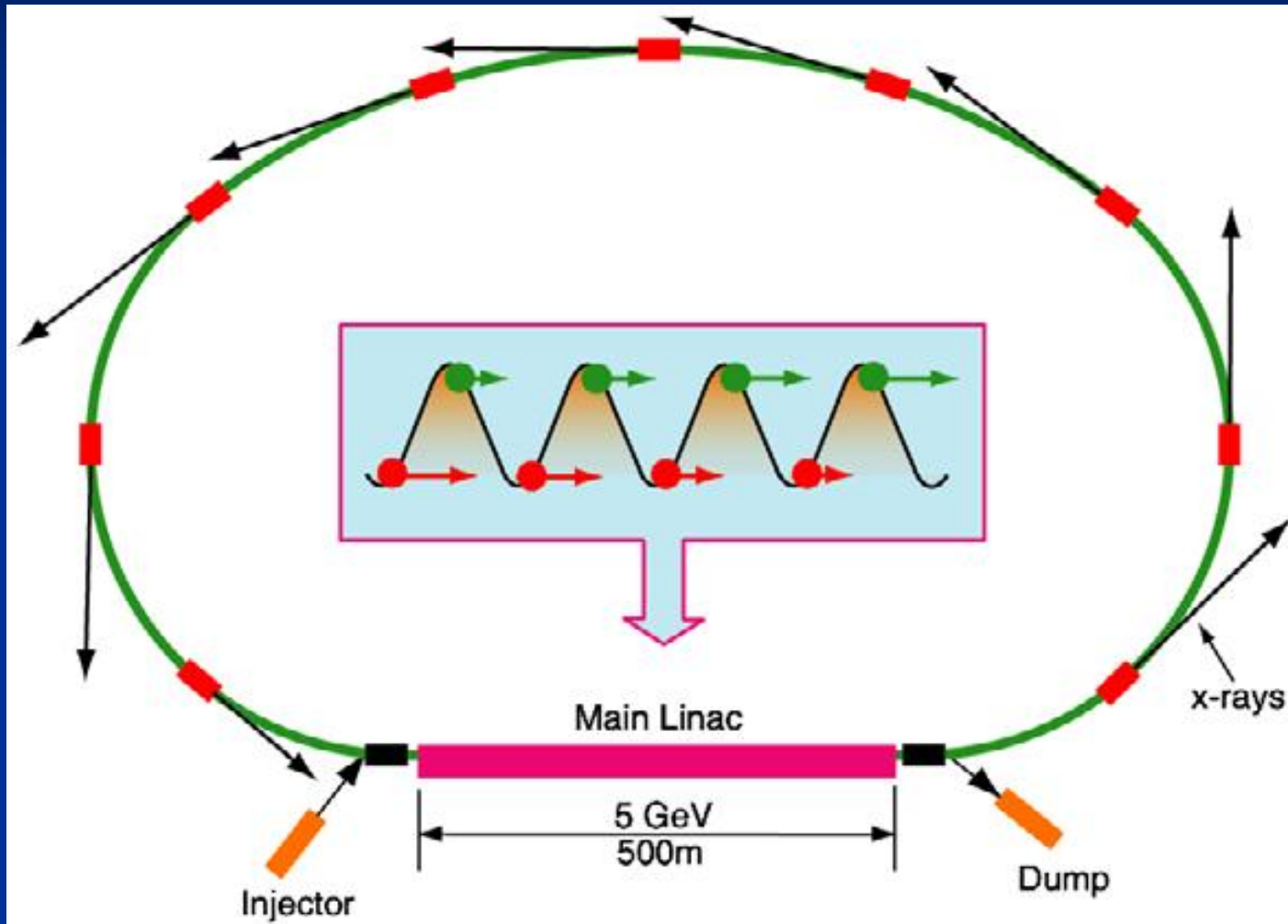
$$B = \frac{F}{(2\pi)^2 \sigma_r^2 \sigma_{r'}^2} = \frac{F}{(\lambda/2)^2}$$

# Towards Diffraction Limit

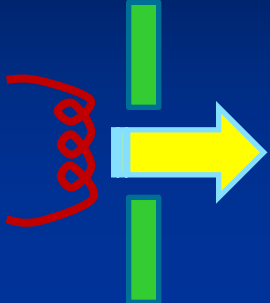




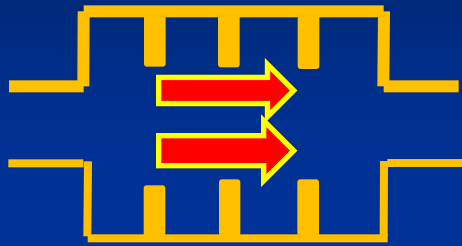
# Energy Recovery Linac



# Adiabatic Damping in Linear Accelerator



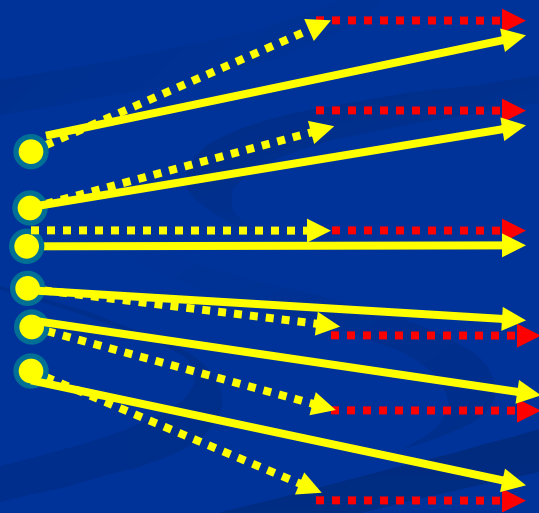
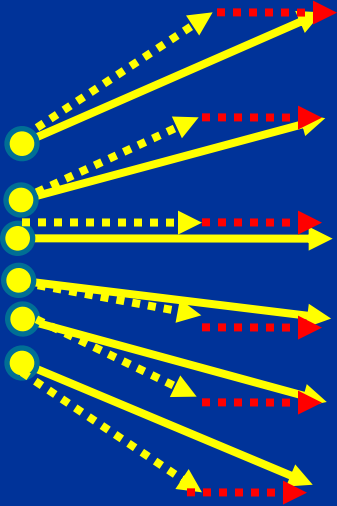
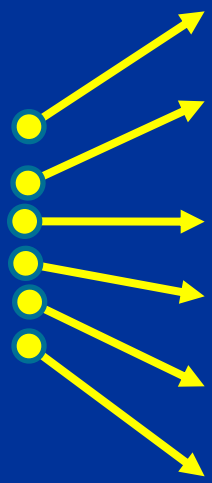
Electron Gun



Accelerating Cavity



Accelerating Cavity



Low emittance e-gun + Acceleration = Ultra-low emittance

# ERL Plan at KEK

<http://pfiqst.kek.jp/ERLoffice/index.html>

Energy region :VUV-X (30eV-30keV)

Brilliance:  $10^{21}$ - $10^{23}$

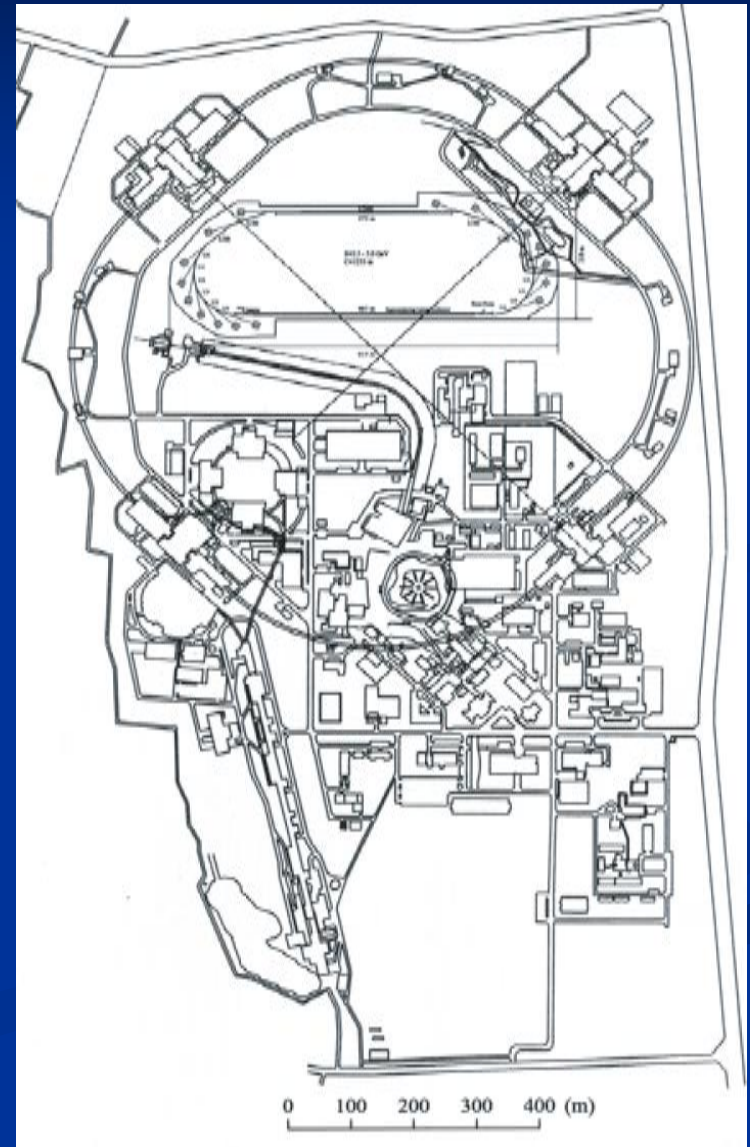
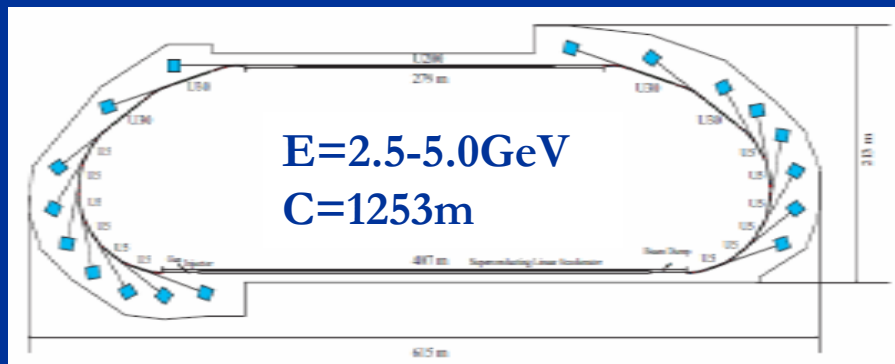
photons/sec/mrad<sup>2</sup>/mm<sup>2</sup>/0.1%B.W. @1~10 keV

Coherent fraction: 10~20% @10keV

Emittance: 10pmrad $\sim\lambda$  /4 $\pi$  @ 10keV

Short pulse: ~100 fs

Number of ID beamlines: ~30 lines

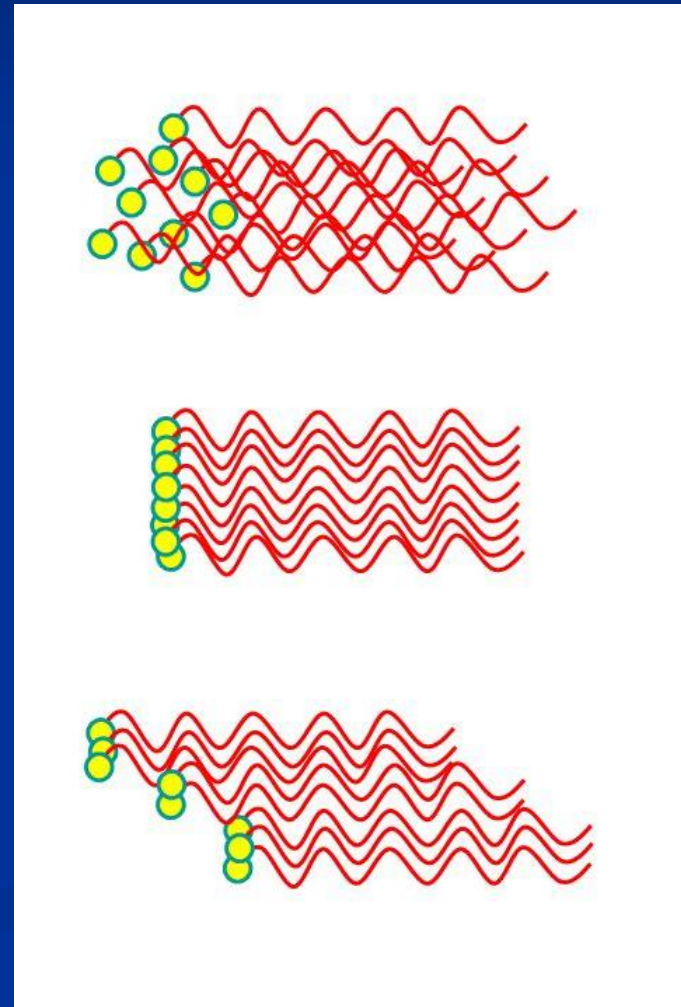


# Towards Coherence

**Incoherent Radiation  
(Normal SR)**

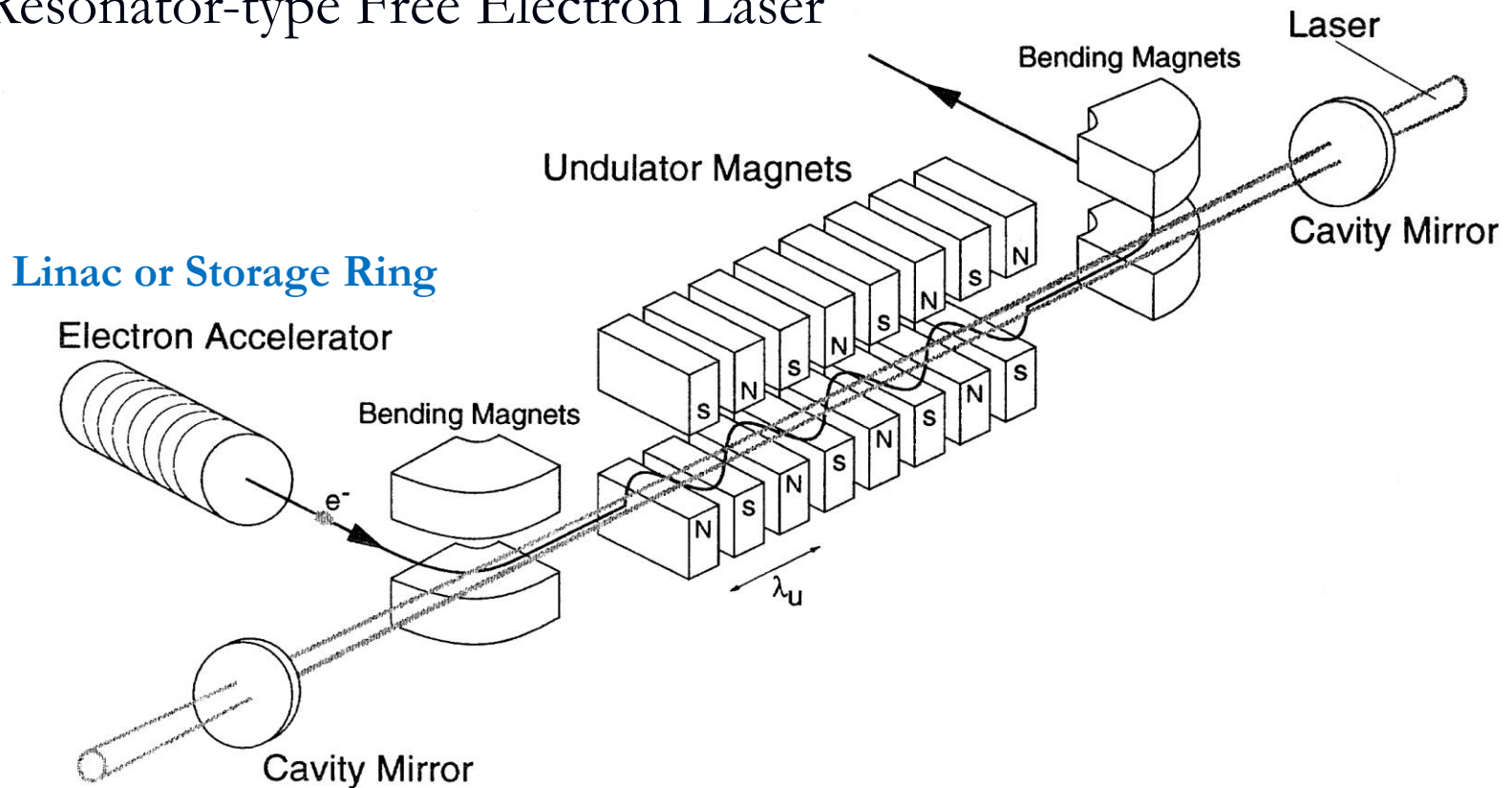
**Coherent Radiation from  
Ultra-short Electron Bunch**

**Coherent Radiation from  
Micro-bunched Electron Beam**



# Free Electron Laser

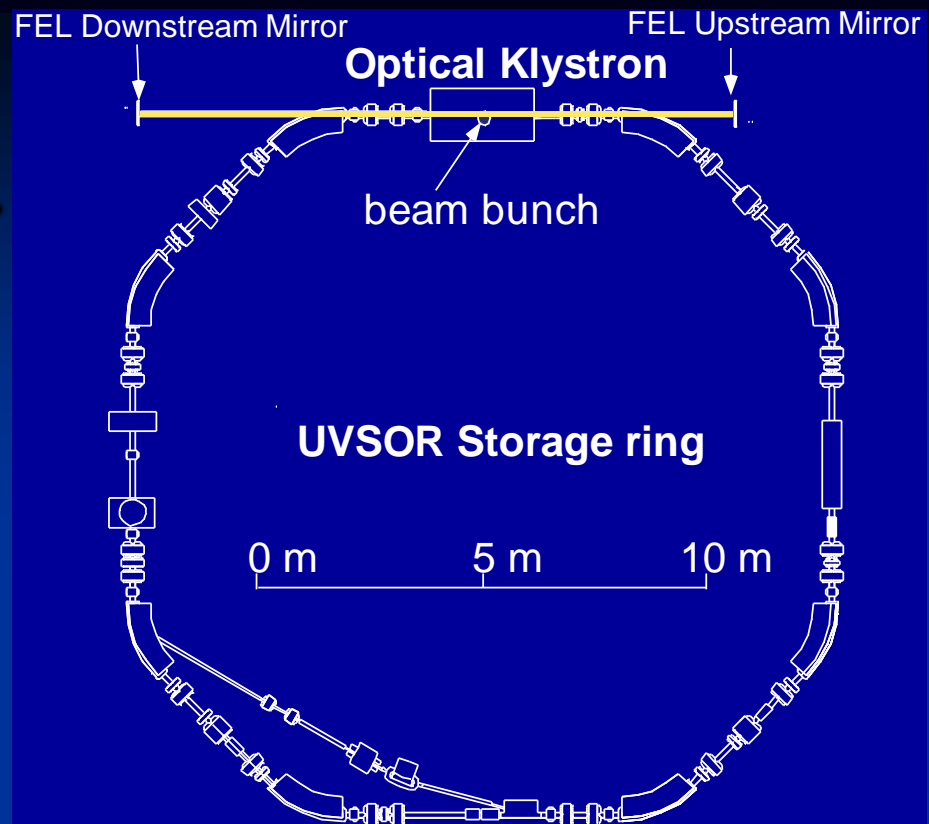
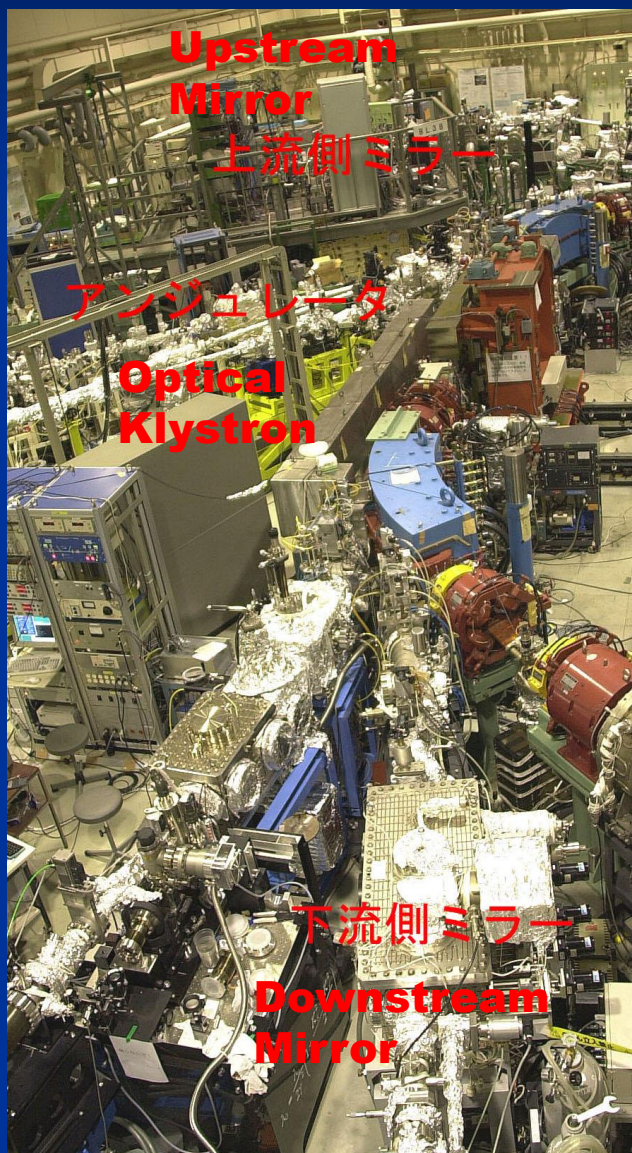
## Resonator-type Free Electron Laser





# UVSOR-II

## Free Electron Laser



### Laser

Wave Length	199~800 nm
Spectral Band Width	$\sim 10^{-4}$
Polarization	Circular/Linear
Pulse Rate	11.26 MHz
Max. Average Power	$\sim 1$ W

### Optical Cavity

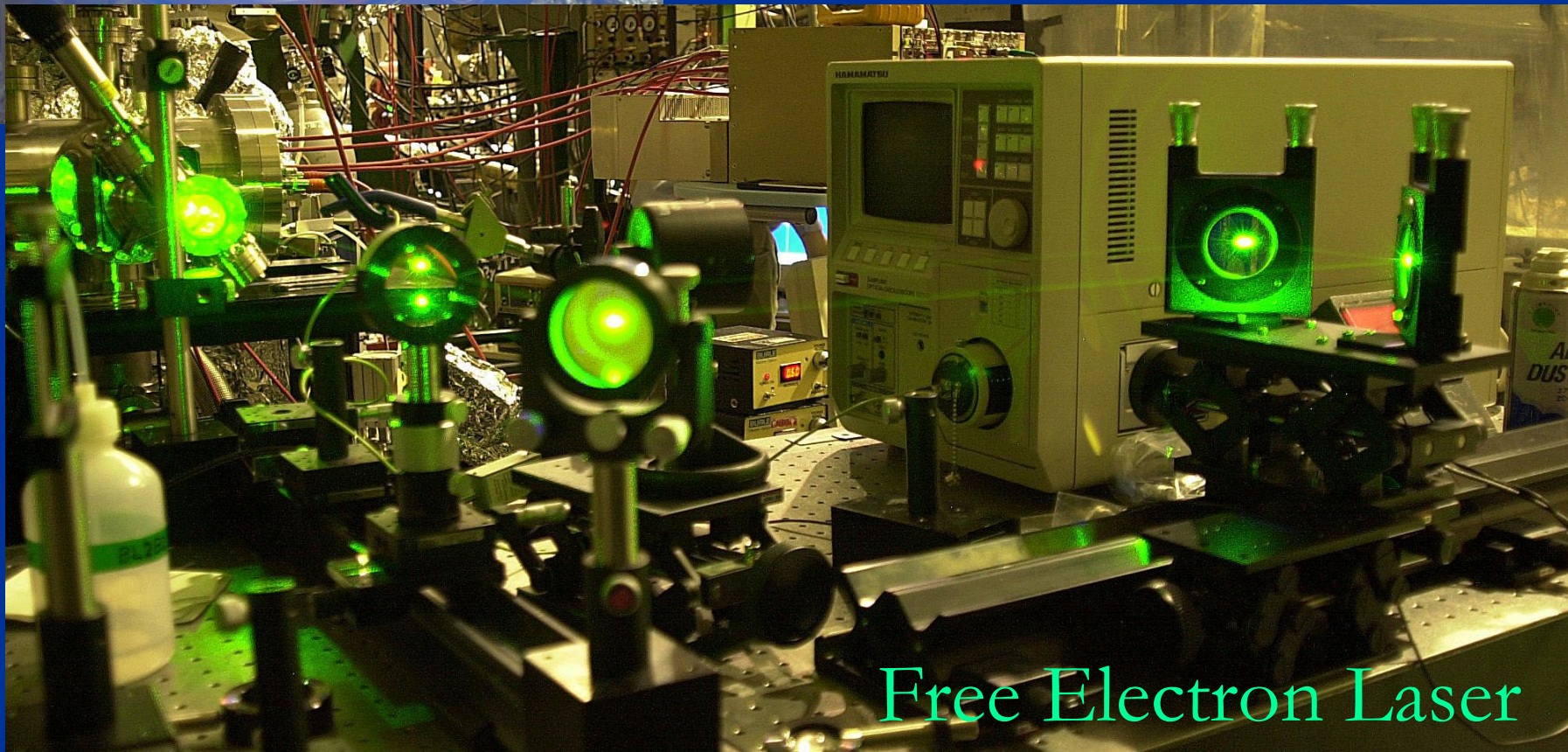
Type	Fabry-Perot
Cavity Length	13.3 m
Mirror	HfO <sub>2</sub> , Ta <sub>2</sub> O <sub>5</sub> , Al <sub>2</sub> O <sub>3</sub> multi-layer

### Optical Klystron

Polarization	Circular/Linear
Length	2.35 m
Period Length	11 cm
Number of Periods	9 + 9



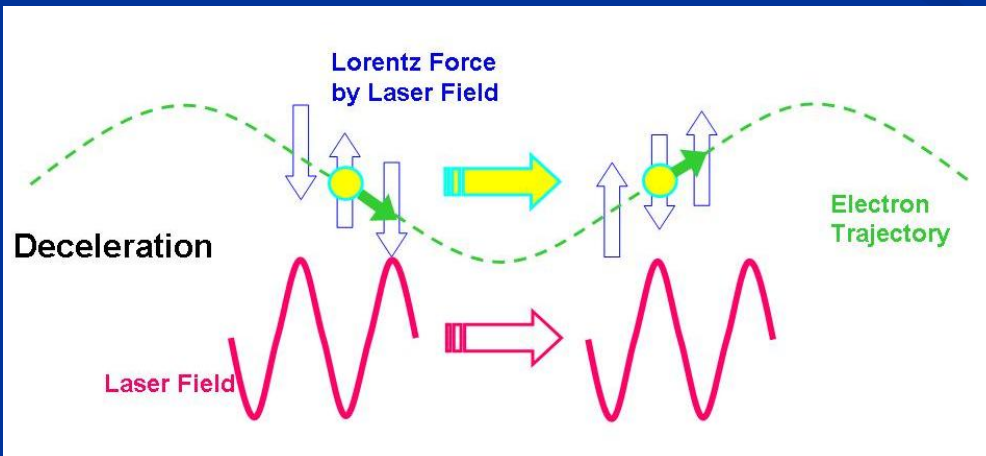
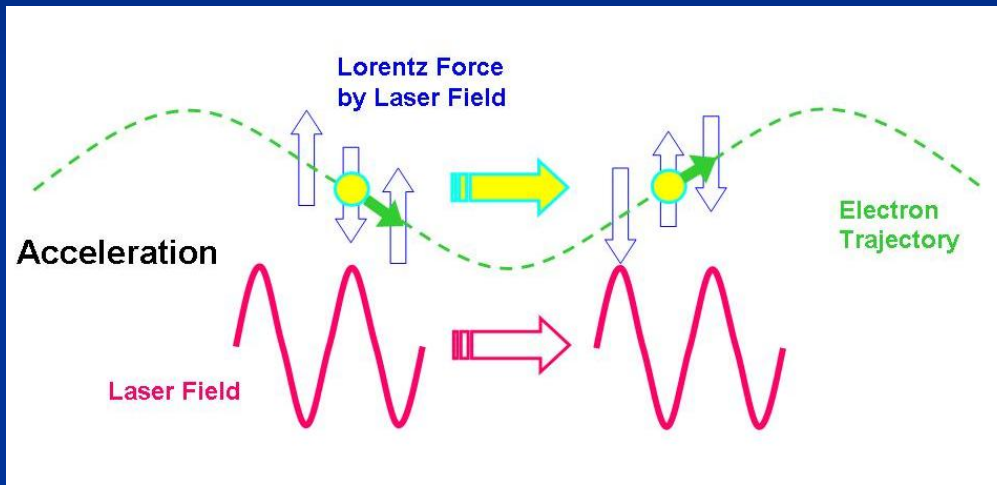
# Synchrotron Radiation



Free Electron Laser

# FEL Process (1)

## Energy Exchange between Electrons and Radiation Field in Undulator



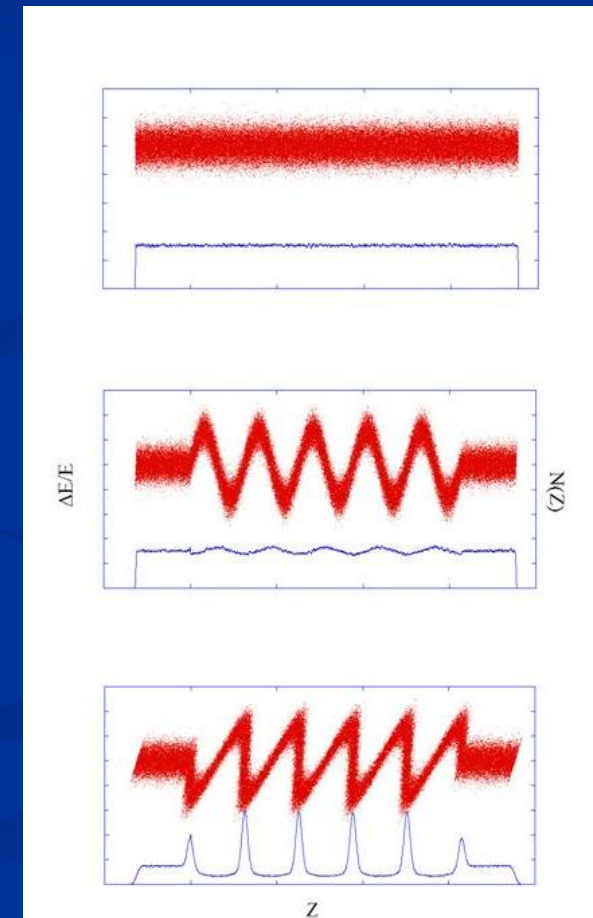
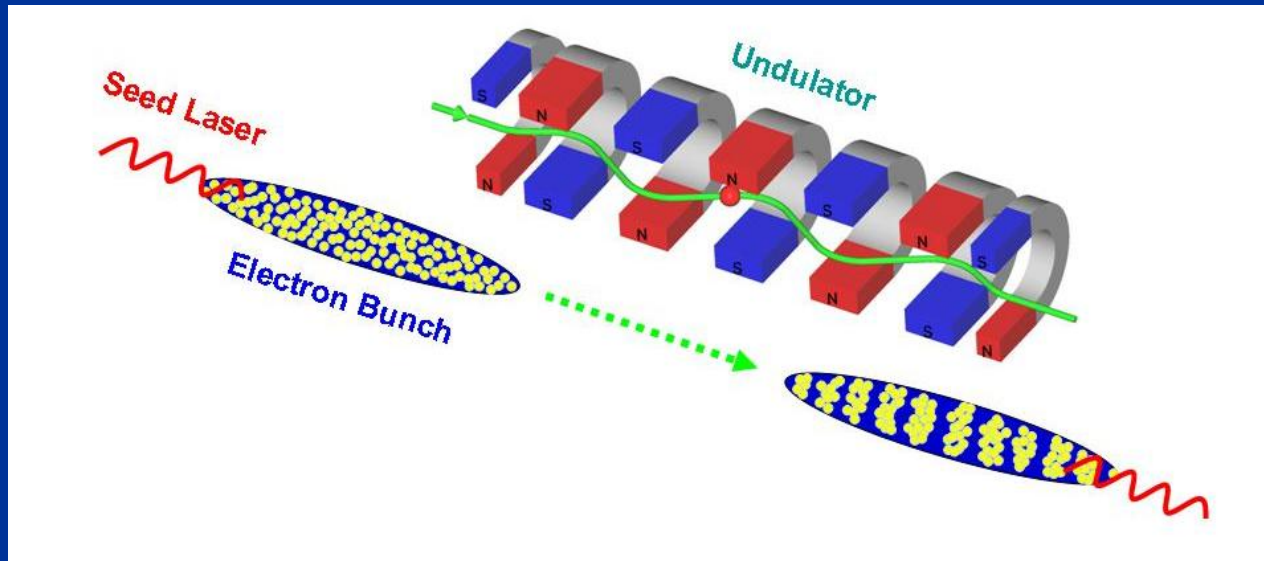
Electrons can be accelerated or decelerated depending on their relative position to the laser field under a resonance condition;

$$\lambda_{laser} = \frac{1 + K^2 / 2}{2\gamma^2} \lambda_{undulator}$$



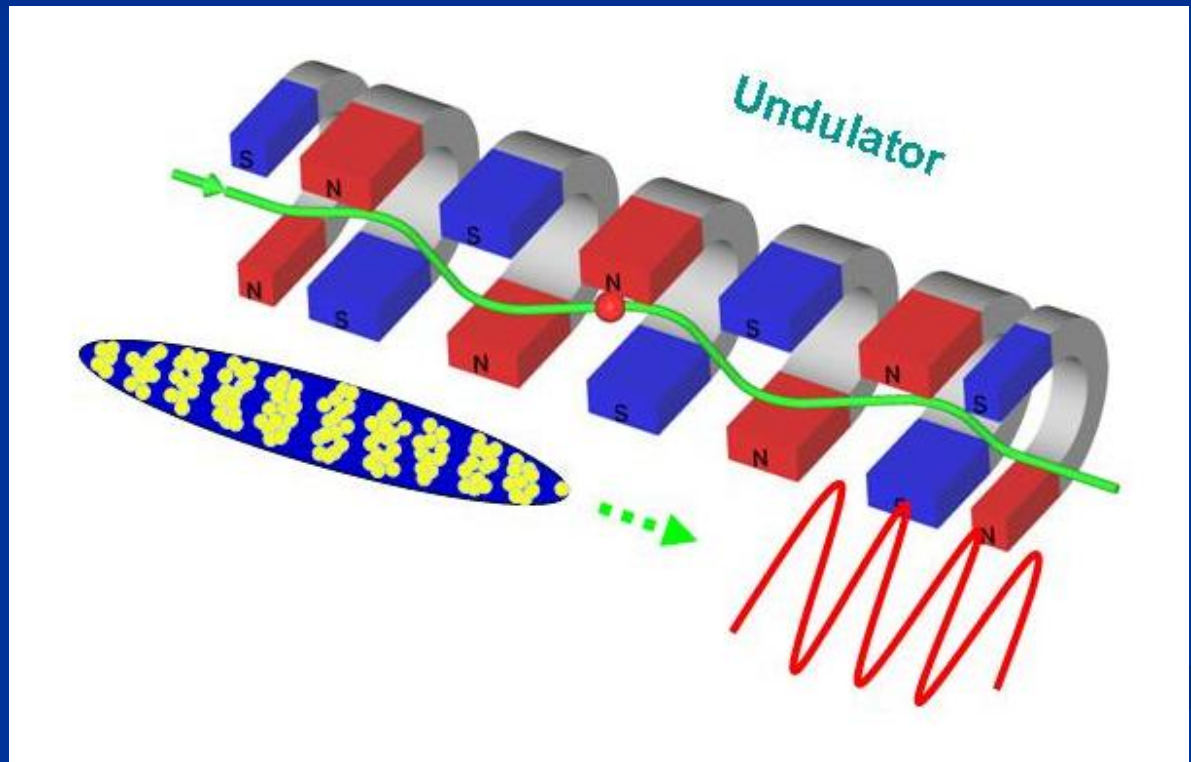
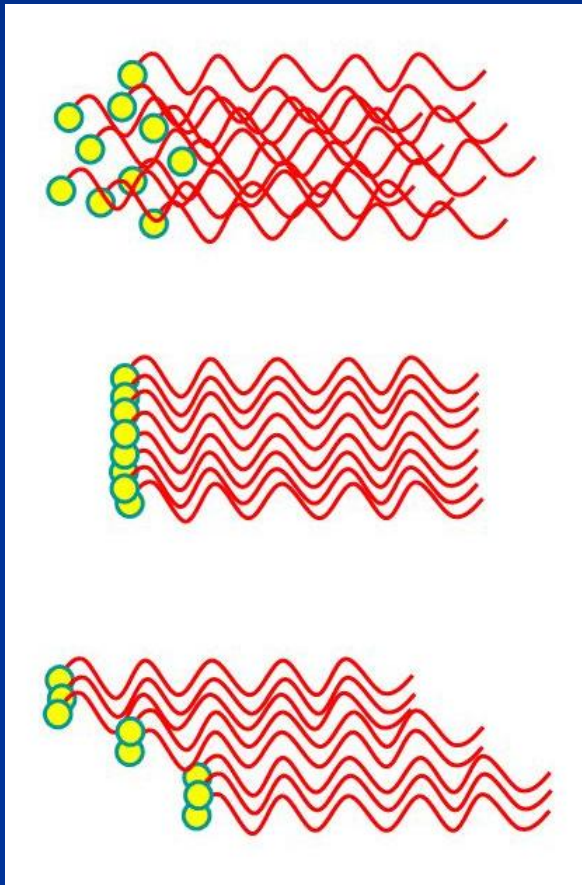
# FEL Process (2)

## Micro-bunching by Laser-Electron Interaction



# FEL Process (3)

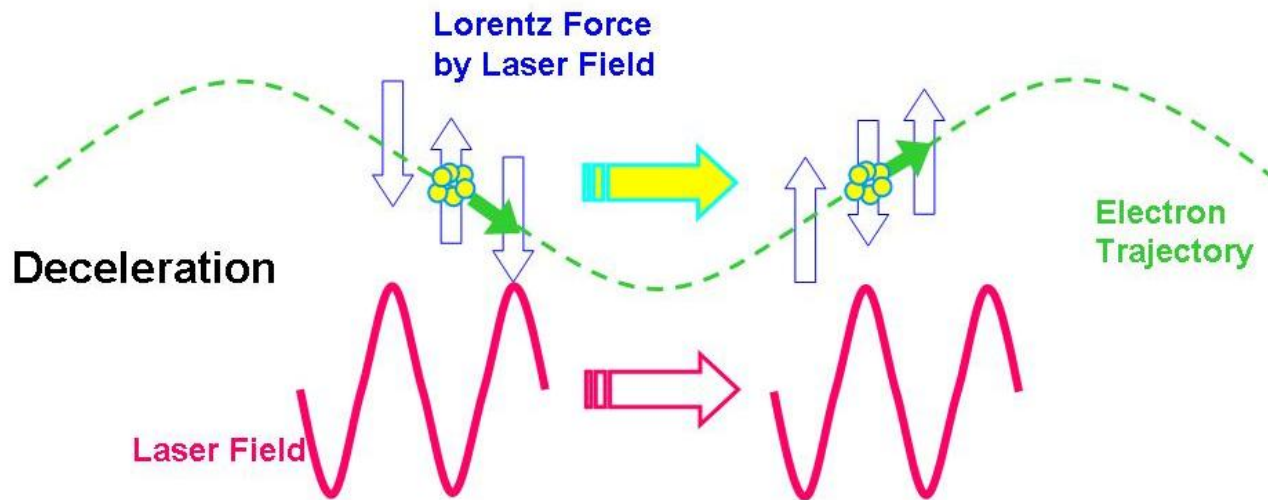
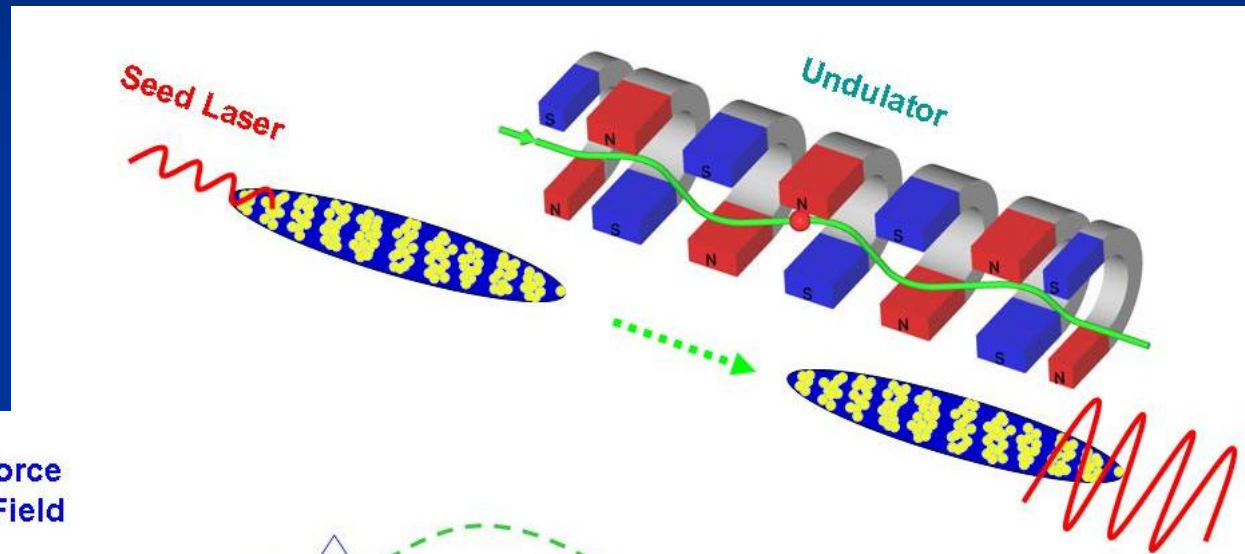
## Coherent Radiation from Micro-bunched Beam





# FEL Process (4)

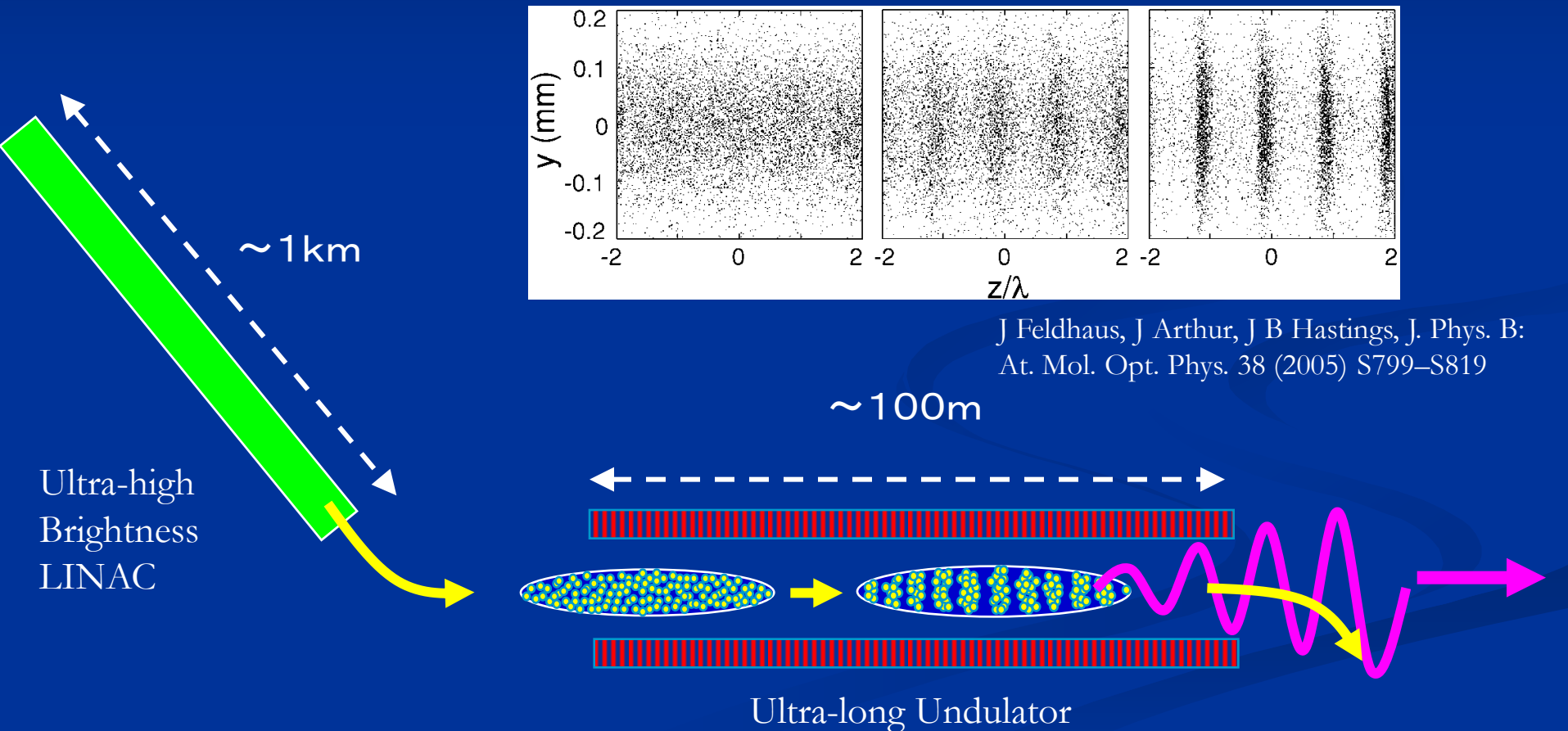
## Amplification of EM field by micro-bunched e-beam



# Free Electron Laser without Optical Cavity

## Single Pass X-ray Free Electron Laser

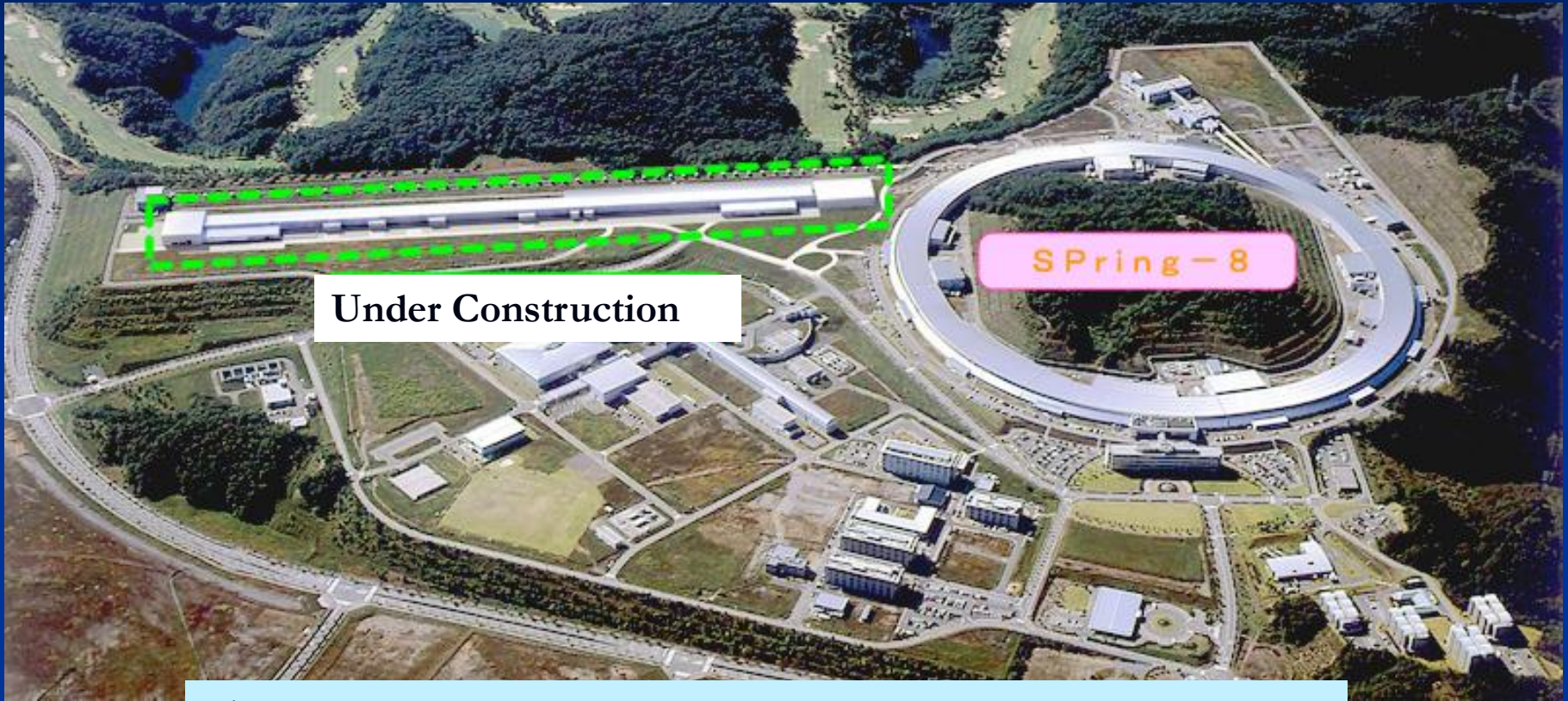
based on Self-Amplified Spontaneous Emission (SASE) Principle



J Feldhaus, J Arthur, J B Hastings, J. Phys. B: At. Mol. Opt. Phys. 38 (2005) S799–S819

# X-ray Free Electron Laser Project in Japan

<http://www.riken.jp/XFEL/eng/whatis/index.html>



Electron Energy	8 GeV
Electron Beam Size	40 micron
X-ray Wavelength	>0.06 nm
X-ray Peak Power	5 GW
X-ray Pulse Length	<100 fsec
X-ray peak Brilliance	$10^{33}$ photons/s/mm <sup>2</sup> /mrad <sup>2</sup> /0.1%b.w.



# シンクロトロン光源

- 電子蓄積リング
  - 安定性、経済性、汎用性
- エネルギー回収型ライナック
  - 回折限界、超短パルス
- シングルパス自由電子レーザー
  - コヒーレント、超短パルス、超高ピークパワー